

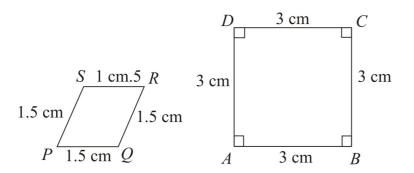
| <b>CBSE NCERT Solutions for Class 10 mathematics Chapter 6</b> |  |
|--|--|
| Exercise 6.1   |  |
| Q.1. All circles are (congruent, similar) similar              |  |
| Solution:  | All circles have the same shape i.e. they are round. But the size of a circle may vary.<br>Thus circles are similar. Each circle has a different radius so the size of the circle may vary.  |
|  | r $R$  |
| Q.2. All squ<br>similar  | ares are (similar, congruent)  |
| Solution:  | We know that,  |
|  | All the sides of a square are equal.   |
|  | Since the ratios of the lengths of their corresponding sides are equal.<br>Hence, all squares are similar since size of squares may be different, but the shape will be always same.   |
| Q.3. All<br>equilateral  | triangles are similar. (Isosceles, equilateral)  |
| Solution:  | We know that, all the sides of an equilateral triangle are equal.  |
|  | IL CONTRACTOR OF |
|  | olygons of the same number of sides are similar, if their corresponding angles are and their corresponding sides are ional. [proportional / equal]   |
| Solution:  | Two polygons of same number of sides are similar, if their corresponding angles are equal and their corresponding sides are proportional.  |
|  | For example, if two triangles with angles 30°,60° and 90° are similar, then the ratio Hypotenuse of 1st circleHypotenuse of 2st circle will be the same.   |
| Q.5. Give tw   | vo different examples of pair of similar figures.  |



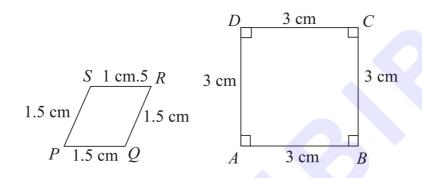
NCERT Mathematics Chapter 6 Triangles Solution: Two figures are said to be similar if the ratio of corresponding sides are equal. Two equilateral triangles with sides 1 cm and 2 cm. D 2 cm 2 cm 1 cm cm 60 60 2 cm Ratio of the corresponding sides are: ABDE=12ACDF=12BCEF=12 Here ratio of the equilateral triangles are same. Therefore, the above figures are similar. Two squares with sides 1 cm and 2 cm. 2 cm 1 cm 2 cm 2 cm R 1 cm 1 cm н C G 2 cm 1 cm Ratio of the corresponding sides are: ABEF=12ACEG=12BDFH=12CDGH=12 Here also ratios of the corresponding sides are equal. Hence, the above two figures are similar. Q.6. Give two different examples of a pair of non-similar figures. Solution: Two figures are said to be non-similar if the ratio of the corresponding sides are not equal. Consider a Trapezium and a square. 3 cm o 3 cm В 4 cr 6 cm 3 cm 3 cm 5 cm 3 cm Ratio of the corresponding sides are: PQAB=3 cm3 cm=1 PSAD=4 3 QRBC=6 cm3 cm=2 SRDC=53 Thus, the ratio of the corresponding sides are not equal. Therefore, figures are not similar. Consider a triangle and a parallelogram Ratio of the corresponding sides are: ACPS=34 BCSR=33=1 3 cm 3 cm 3 cm 4 cm 4 cm 3 cm 3 cm Hence, the above two figures are non-similar.



Q.7. State whether the following quadrilaterals are similar or not.



Solution:



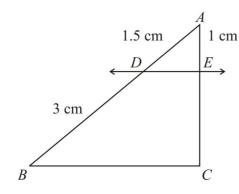
To check whether the given quadrilaterals are similar or not we need to check the ratio of the corresponding sides and angles.

Corresponding sides of two quadrilaterals are proportional i.e., 1:2 but their corresponding angles are not equal. Hence, quadrilaterals PQRS and ABCD are not similar.

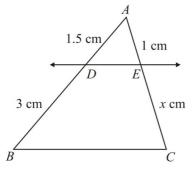


# Exercise 6.2

Q.1. In the figure given below, DE BC. Find EC.

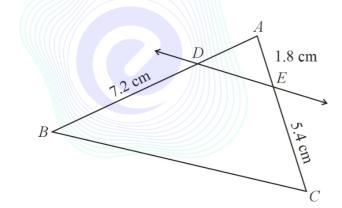


## Solution:

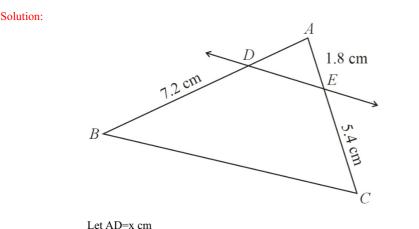


Let EC=x cm Since DEIBC So, using basic proportionality theorem we get: ADDB=AEEC  $\Rightarrow 1.53=1x$  $\Rightarrow x=3\times11.5$  $\Rightarrow x=2$ Hence, EC=2 cm.

Q.2. In Fig. DEIBC. Find AD







- Let AD=x cm Since DE BC Hence, using Basic proportionality theorem, ADDB=AEEC  $\Rightarrow x7.2=1.85.4$  $\Rightarrow x=2.4$  cm Hence, AD=2.4 cm
- Q.3. The diagonals of a quadrilateral ABCD intersect each other at the point O such that AOBO=CODO. Show that ABCD is a trapezium.

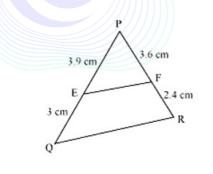


Draw a line segment OEIAB In  $\triangle ABC$ Since, OEIAB. Hence, AOOC=BEEC.

But by the given relation, we have: AOBO=CODO  $\Rightarrow AOOC=OBOD$ Hence, OBOD=BEEC So, using converse of basic proportionality theorem, EOIDC. Therefore, ABIOEIDC  $\Rightarrow ABICD$ Therefore, ABCD is a trapezium.

Q.4. E and F are points on the sides PQ and PR respectively of a  $\triangle$  PQR. State whether EFIQR where PE=3.9 cm, EQ=3 cm, PF=3.6 cm and FR=2.4 cm.

Solution:



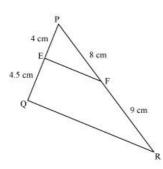
Given: PE=3.9 cm, EQ=3 cm, PF=3.6 cm and FR=2.4 cm Now, PEEQ=3.93=1.3

PFFR=3.62.4=1.5 Since, PEEQ≠PFFR Hence, EF is not parallel to QR.



Q.5. E and F are points on the sides PQ and PR respectively of a △PQR. For each of the following cases, state whether EFIQR: PE=4 cm, QE=4.5 cm, PF=8 cm and RF=9 cm

## Solution:



Given, PE=4 cm, QE=4.5 cm, PF=8 cm, RF=9 cm PEEQ=44.5=89

PFFR=89 Since PEEQ=PFFR Hence, EFIQR (using Basic proportionality theorem)

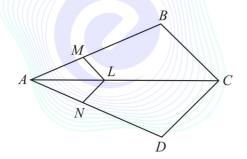
Q.6. E and F are points on the sides PQ and PR respectively of a  $\Delta$ PQR. For each of the following cases, state whether EFIQR:

PQ=1.28 cm, PR=2.56 cm, PE=0.18 cm and PF=0.36 cm

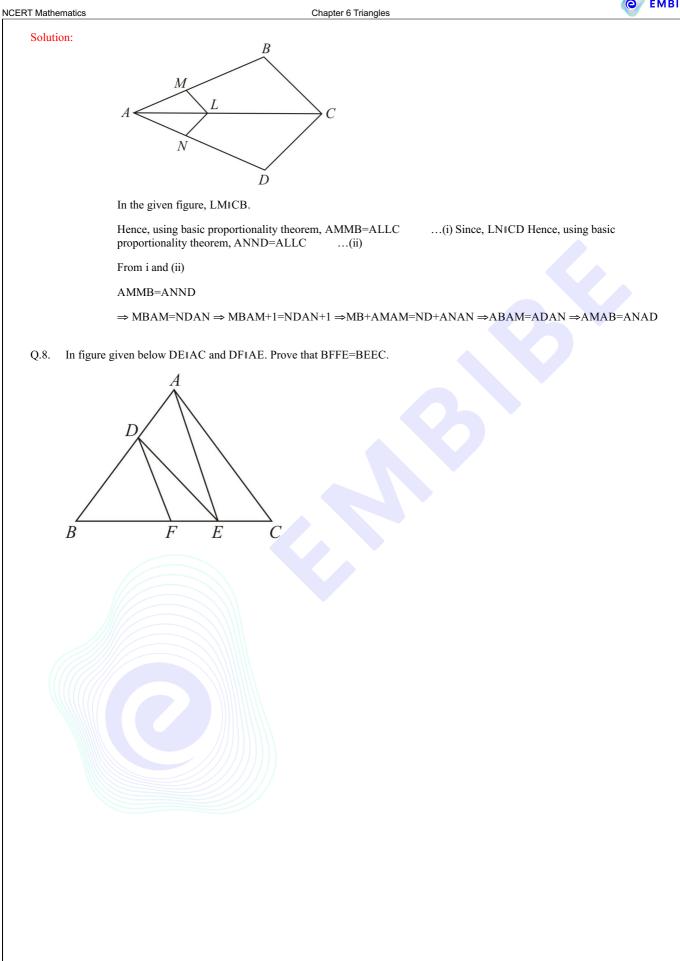
# Solution:

Given, PQ=1.28 cm, PR=2.56 cm, PE=0.18 cm and PF=0.36 cm EQ=PQ-PE=1.28-0.18=1.1 cm and FR=PR-PF=2.56-0.36=2.2 cm PEEQ=0.181.1=18110=955 PFFR=0.362.2=955 Since, PEEQ=PFFR Hence, EFIQR (using basic proportionality thorem)

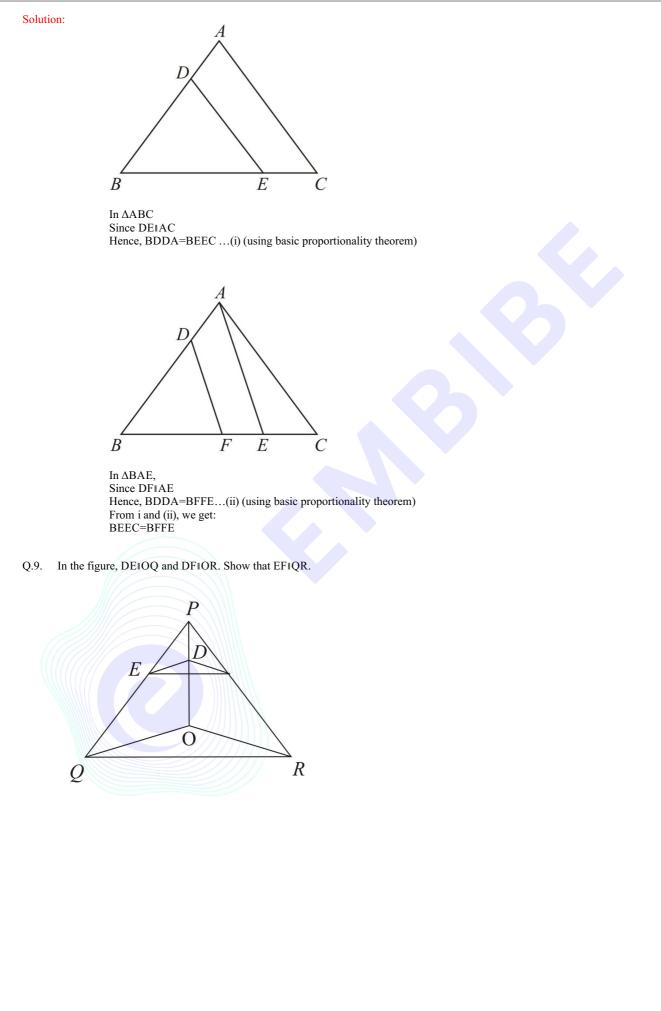
Q.7. In the figure, if LMICB and LNICD, prove that AMAB=ANAD



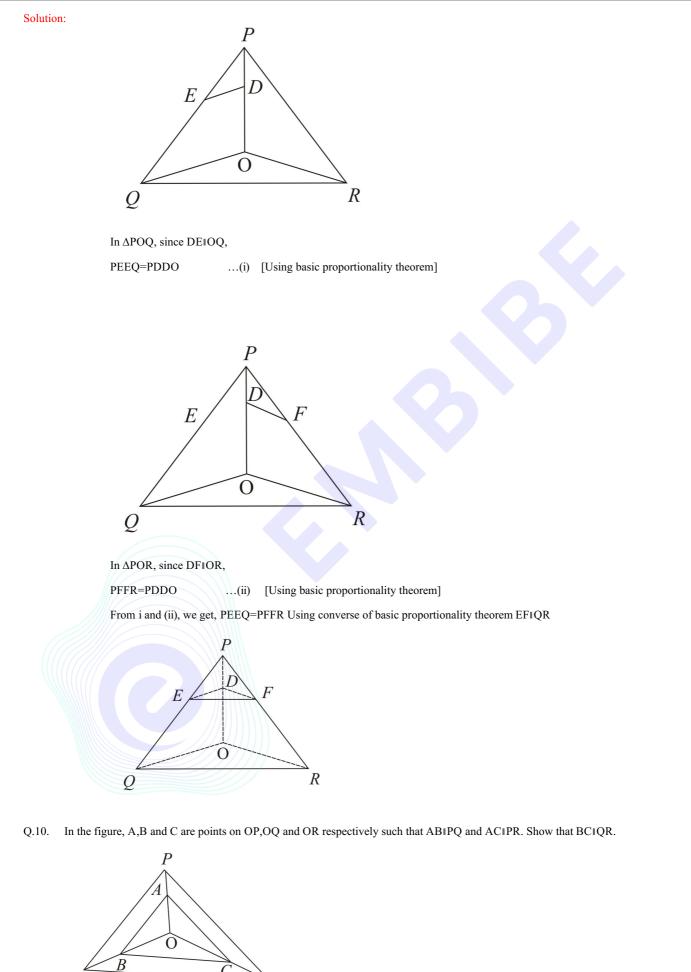










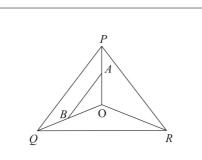


Q

R



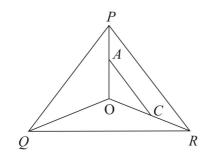
Chapter 6 Triangles



In  $\triangle POQ$ 

Since, ABIPQ, Hence, OAAP=OBBQ

...(i) [Using basic proportionality theorem]



In  $\triangle POR$ 

Since, ACIPR Hence, OAAP=OCCR

...(ii) [Using basic proportionality theorem]

From i and (ii)

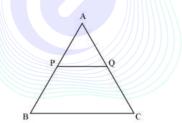
OBBQ=OCCR

Hence, BCIQR (Using converse of basic proportionality theorem)

$$P$$
  
 $B$   $O$   $C$   
 $R$ 

Q.11. Using Theorem 6.1, prove that a line drawn through the midpoint of one side of a triangle parallel to another side bisects the third side. (Recall that you have proved it in Class IX).

Solution:

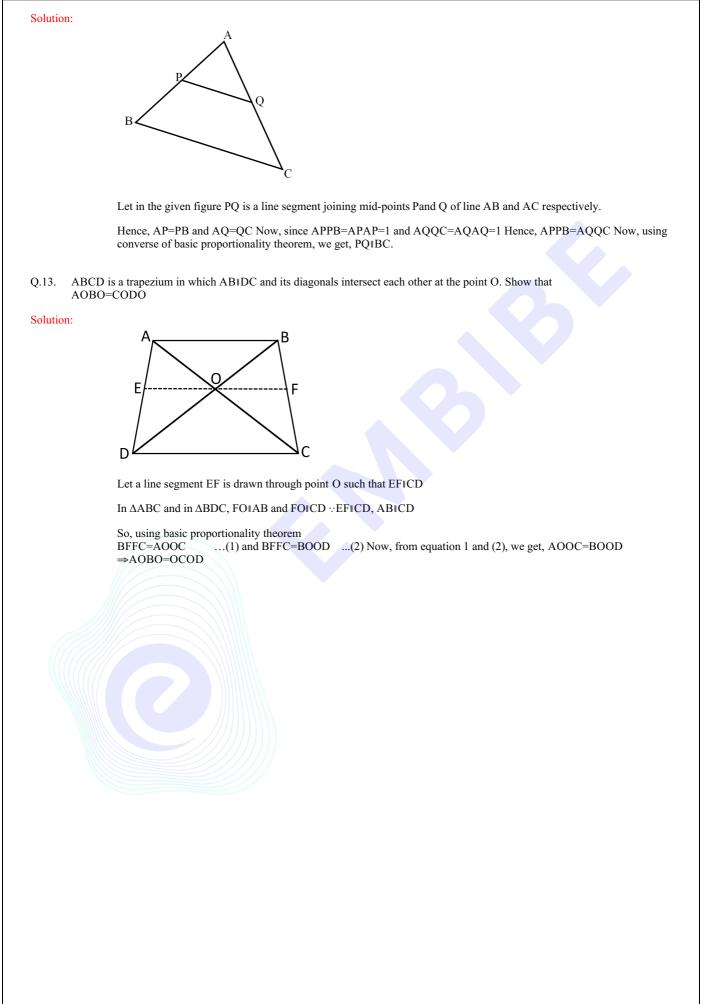


Let in the given figure PQ is a line segment drawn through mid-point P of line AB such that PQIBC Hence, AP=PB

Now, using basic proportionality theorem AQQC=APPB  $\Rightarrow AQQC=APAP$   $\Rightarrow AQQC=1$   $\Rightarrow AQ=QC$ Hence, Q is the mid-point of AC.

Q.12. Prove that the line joining the mid-points of any two sides of a triangle is parallel to the third side.

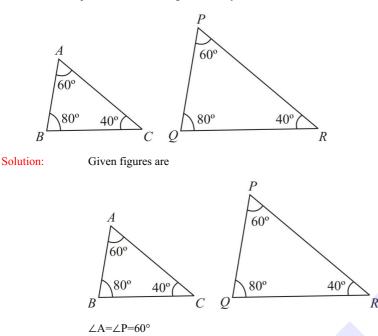




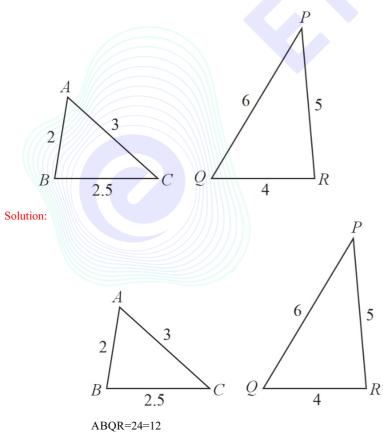


## Exercise 6.3

Q.1. State which pairs of triangles in the figure are similar. Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



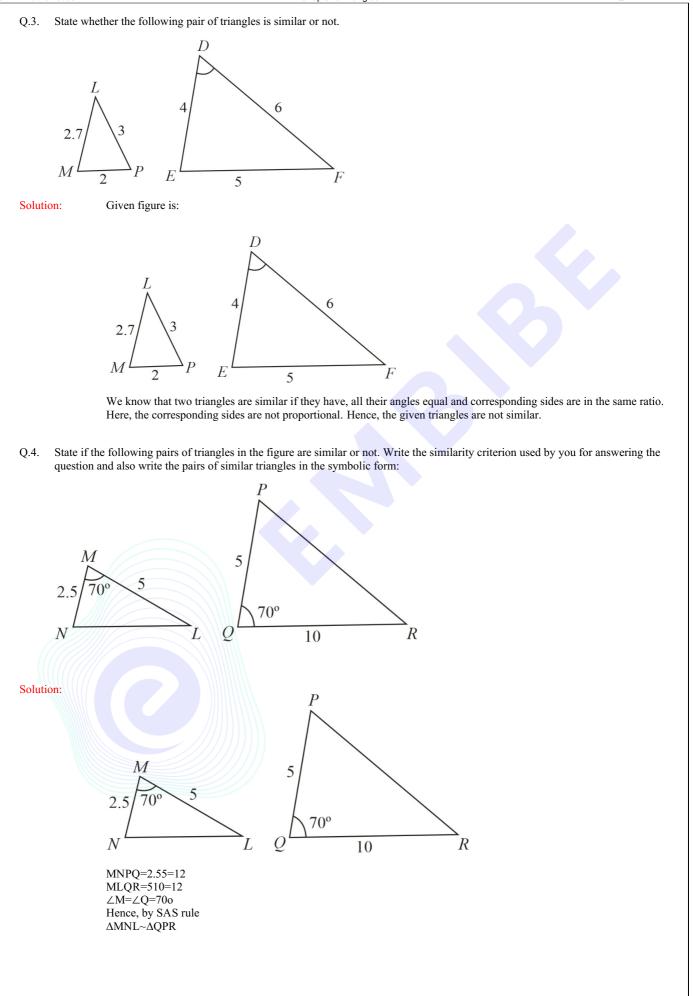
- $\angle B = \angle Q = 80^{\circ} \angle C = \angle R = 40^{\circ}$  Hence by AAA rule  $\triangle ABC \sim \triangle PQR$ .
- Q.2. Are the pairs of triangles in the figure similar? Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



BCRP=2.55=12 CAPQ=36=12 Since, ABQR=BCRP=CAPQ Hence, by SSS rule. ΔABC~ΔQRP.

Chapter 6 Triangles



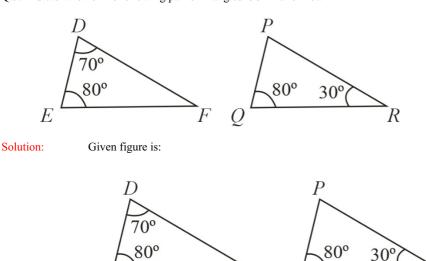


Chapter 6 Triangles



Q.5. State whether the following pair of triangles is similar or not.

E

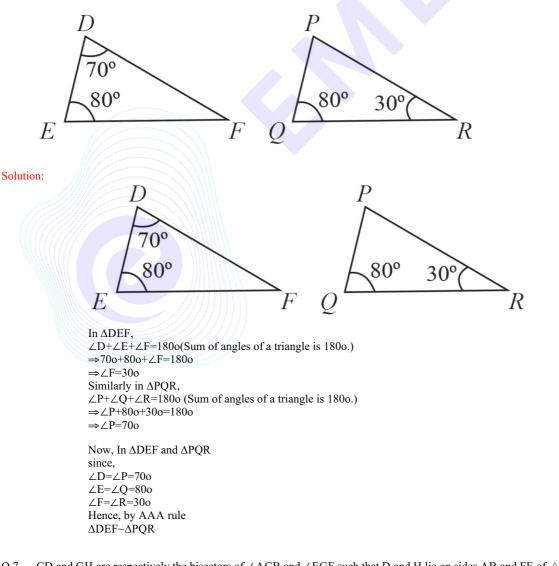


We know that two triangles are said to be similar if their corresponding angles are congruent and the corresponding sides are in proportion. In other words, similar triangles are the same shape, but not necessarily the same size. Here, as the corresponding sides are not in proportional. Hence, the given triangles is not similar.

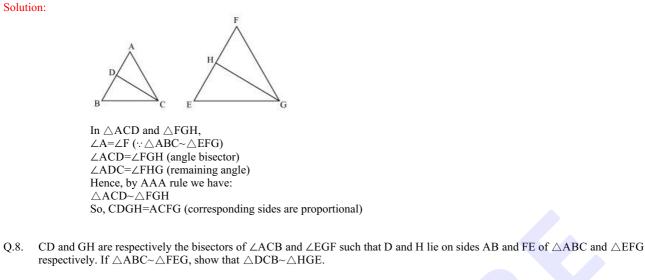
R

Q.6. State whether the pair triangles are similar or not. Write the similarity criterion used by you for answering the question and also write the pair of similar triangles in the symbolic form.

Q



Q.7. CD and GH are respectively the bisectors of  $\angle ACB$  and  $\angle EGF$  such that D and H lie on sides AB and FE of  $\triangle ABC$  and  $\triangle EFG$  respectively. If  $\triangle ABC \sim \triangle FEG$ , show that CDGH=ACFG.



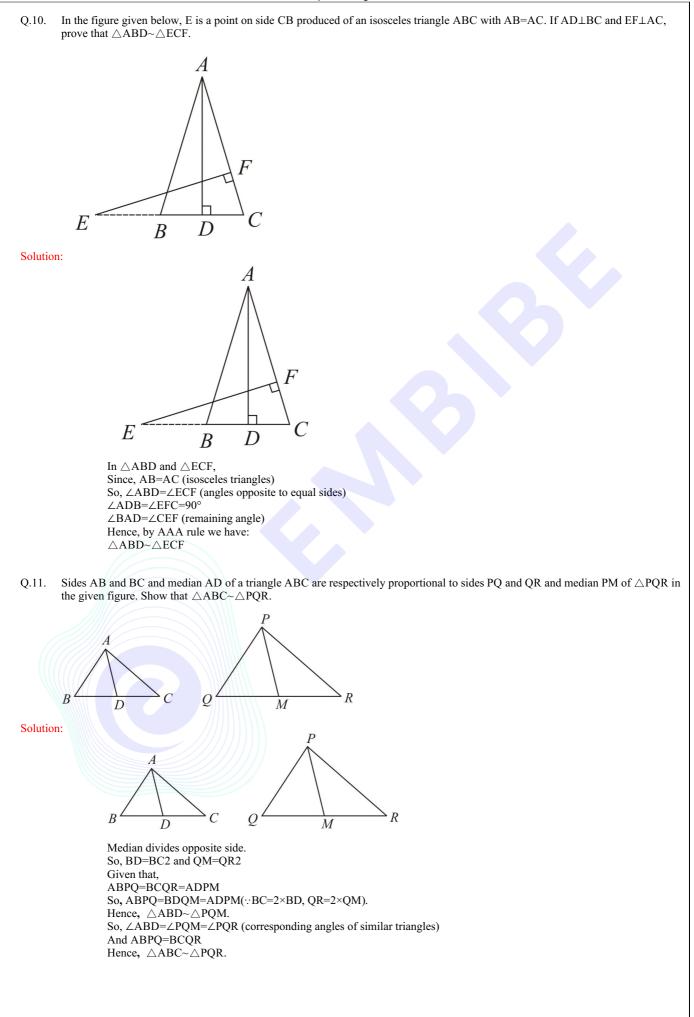
Since  $\triangle ABC \sim \triangle FEG$ Hence,  $\angle A = \angle F$  $\angle B = \angle E$  $\angle ACB = \angle FGE$  $\Rightarrow \angle ACB = \angle FGE 2$ And  $\angle DCB = \angle HGE$  (angle bisector)  $\angle BDC = \angle EHG$  (remaining Angle) Hence, by AAA rule we have:  $\triangle DCB \sim \triangle HGE$ 

Q.9. CD and GH are respectively the bisectors of  $\angle ACB$  and  $\angle EGF$  such that D and H lie on sides AB and FE of  $\triangle ABC$  and  $\triangle EFG$  respectively. If  $\triangle ABC \sim \triangle FEG$ , show that  $\triangle DCA \sim \triangle HGF$ 

Solution:

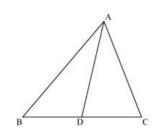
Since  $\triangle ABC \sim \triangle FEG$ Hence,  $\angle A = \angle F$  $\angle B = \angle E$  $\angle ACB = \angle FGE$  $\Rightarrow \angle ACB = \angle FGE$  $\Rightarrow \angle ACD = \angle FGH$  (angle bisector)  $\angle CDA = \angle GHF$  (remaining angle) Hence, by AAA rule we have:  $\triangle DCA \sim \triangle HGF$ 



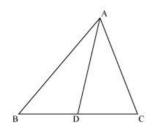




Q.12. D is a point on the side BC of a triangle ABC such that  $\angle ADC = \angle BAC$ . Show that CA2=CB.CD.

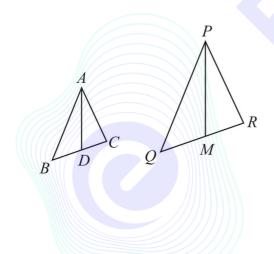


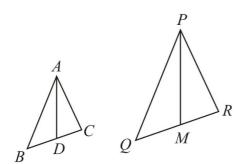
Solution:



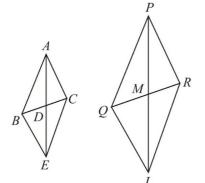
In  $\triangle ACD$  and  $\triangle BAC$ It is given that  $\angle ADC = \angle BAC$  $\angle ACD = \angle BCA$  (common angle)  $\angle CAD = \angle CBA$  (remaining angle) Hence, by AAA rule we have:  $\triangle ADC \sim \triangle BAC$ So, by corresponding sides of similar triangles will be proportional to each other. CACB=CDCA Hence, CA2=CB×CD.

Q.13. Sides AB and AC and median AD of a triangle ABC are respectively proportional to sides PQ and PR and median PM of another triangle PQR. Show that  $\triangle ABC \sim \triangle PQR$ .





Given that, ABPQ=ACPR=ADPM



Let us extend AD and PM up to point E and L respectively such that AD=DE and PM=ML. Now join B to E, C to E, Q to L and R to L. We know that medians divide opposite sides. So, BD=DC and QM=MR Also, AD=DE (by construction) And PM=ML(By construction) So, in quadrilateral ABEC, diagonals AE and BC bisects each other at point D. Also, in quadrilateral PQLR, diagonals PL and QR bisects each other at point M. So, quadrilaterals ABED and PQLR are parallelograms. AC=BE and AB=EC (Since it is a parallelogram, opposite sides will be equal) Also PR=QL and PQ=LR (Since it is a parallelogram, opposite sides will be equal)

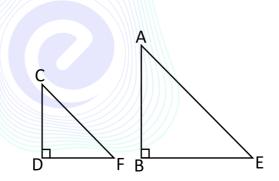
In  $\triangle ABE$  and  $\triangle PQL$ ,

ABPQ=BEQL=AEPL (ACPR=BEQL and ADPM=2AD2PM=AEPL)

Hence, by SSS rule,  $\triangle ABE \sim \triangle PQL$  Similarly,  $\triangle AEC \sim \triangle PLR$  Hence,  $\angle BAE = \angle QPL$  and  $\angle EAC = \angle LPR$  Hence,  $\angle BAC = \angle QPR$  Now, in  $\triangle ABC$  and  $\triangle PQR$ , ABPQ = ACPR and  $\angle BAC = \angle QPR$  Hence, by SAS rule,  $\triangle ABC \sim \triangle PQR$ 

Q.14. A vertical pole of length 6 m casts a shadow 4 m long on the ground and at the same time a tower casts a shadow 28 m long. Find the height of the tower.





Let AB be a tower and CD be a pole

Shadow of AB is BE. Shadow of CD is DF. The sun ray will fall on tower and pole at same angle.  $\therefore \angle DCF = \angle BAE$  and  $\angle DFC = \angle BEA \angle CDF = \angle ABE = 900$  (Tower and pole are vertical to ground) Hence, by AAA rule,  $\triangle ABE \sim \triangle CDF$ Therefore ABCD=BEDF  $\Rightarrow AB6 = 284 \Rightarrow AB = 42$  Hence, the height of the tower =42 meters.

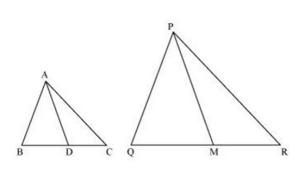
Q.15. If AD and PM are medians of triangles ABC and PQR, respectively where  $\triangle ABC \sim \triangle PQR$ , prove that ABPQ=ADPM

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Chapter 6 Triangles







Since  $\triangle ABC \sim \triangle PQR$ 

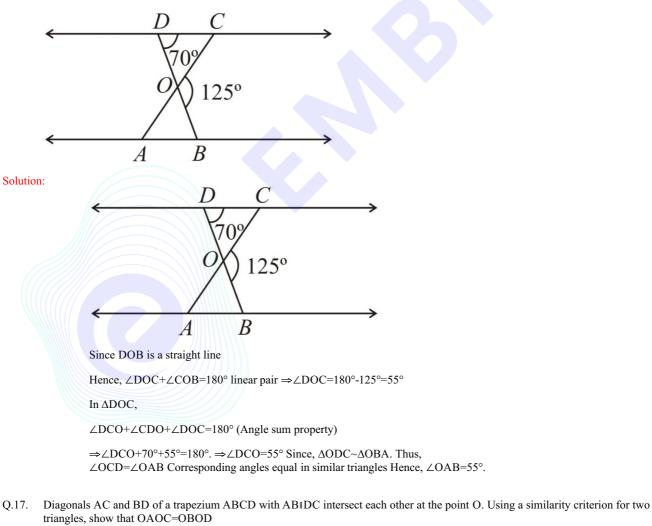
Thus, their respective sides will be in proportion Or, ABPQ=ACPR=BCQR ...(1) Also,  $\angle A = \angle P, \angle B = \angle Q, \angle C = \angle R...(2)$  Since, AD and PM are medians, they will divide their opposite sides equally. Hence, BD=BC2 and QM=QR2...(3)

From equation 1 and (3)

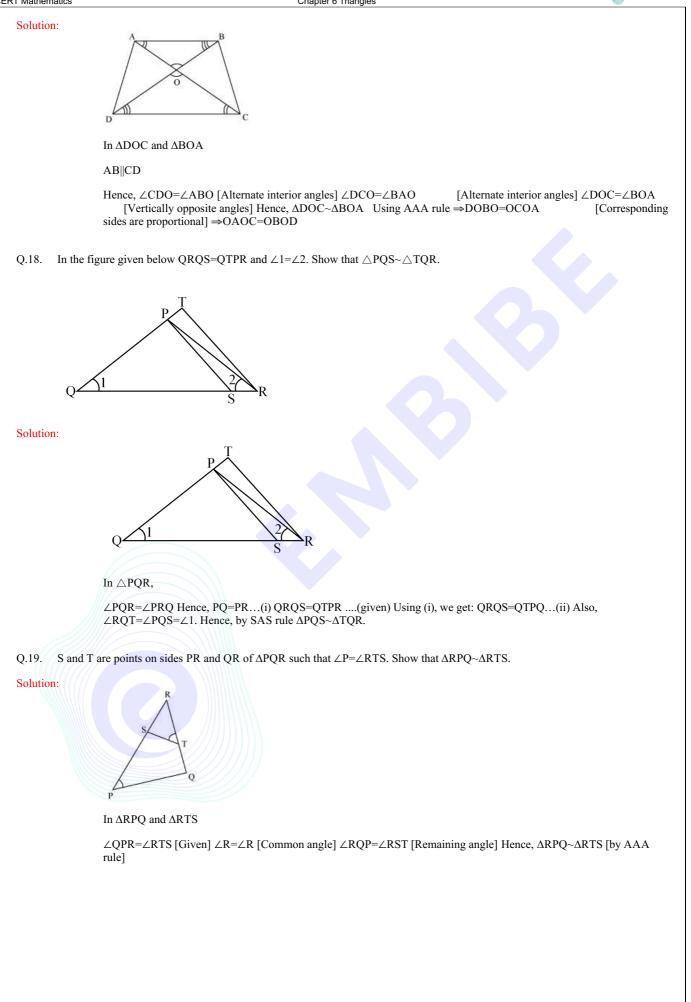
ABPQ=BDQM

 $\angle B = \angle Q$  (From equation 2) Hence, by SAS rule,  $\triangle ABD \sim \triangle PQM$  Hence, ABPQ = ADPM (Corresponding sides are proportional)

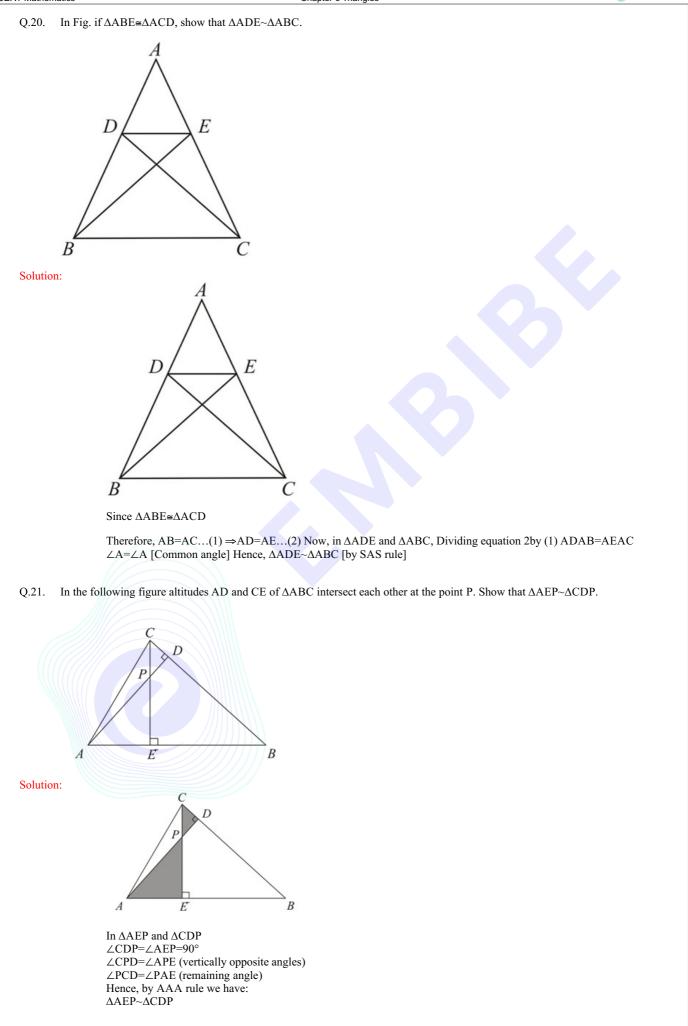
Q.16. In the following figure,  $\triangle ODC \sim \triangle OBA$ ,  $\angle BOC = 125 \circ$  and  $\angle CDO = 70 \circ$ . Find  $\angle DOC$ ,  $\angle DCO$  and  $\angle OAB$ .



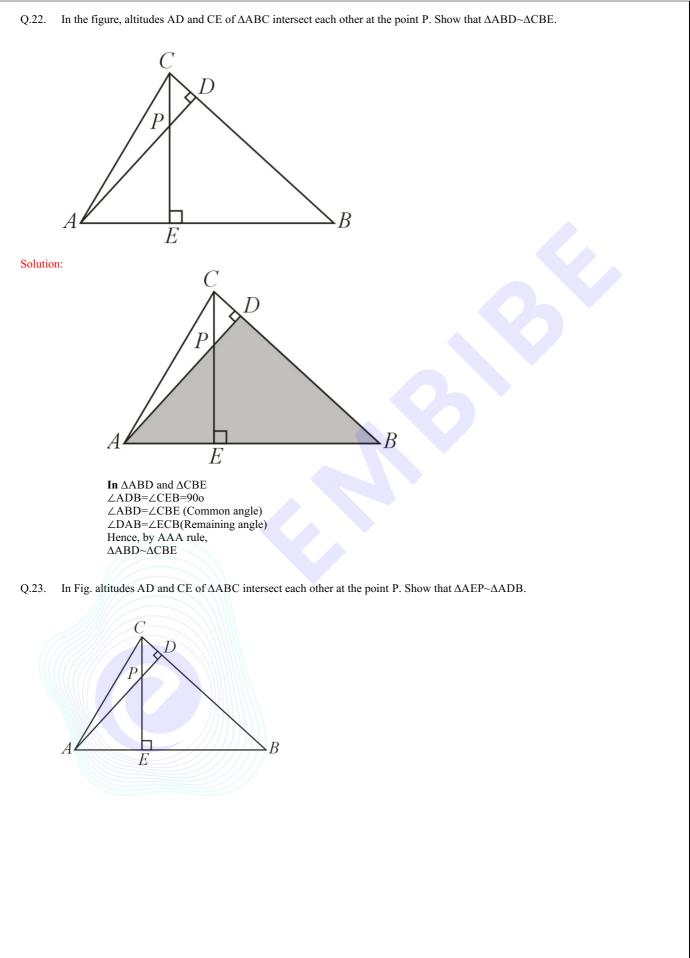




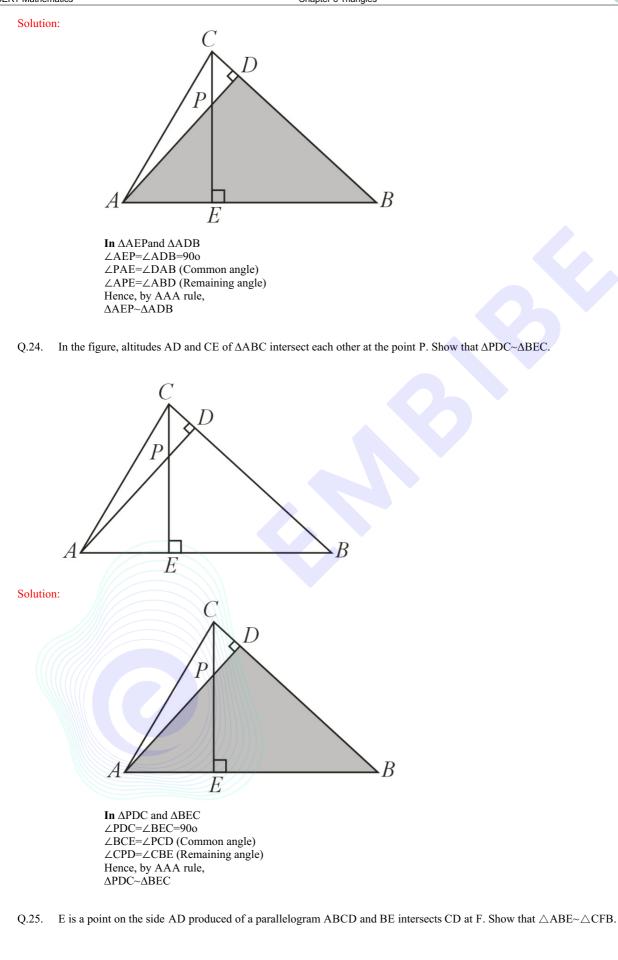






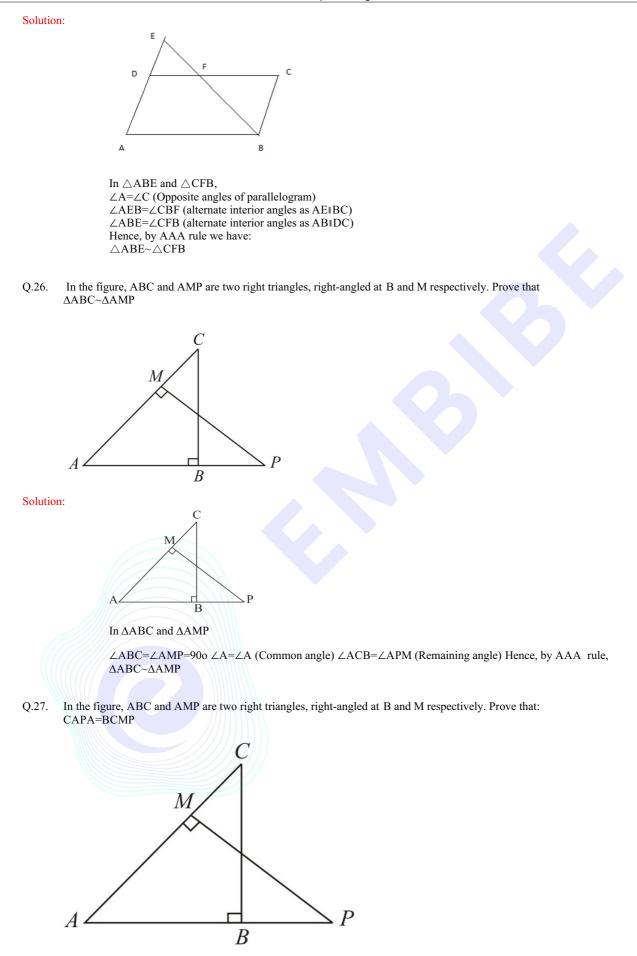




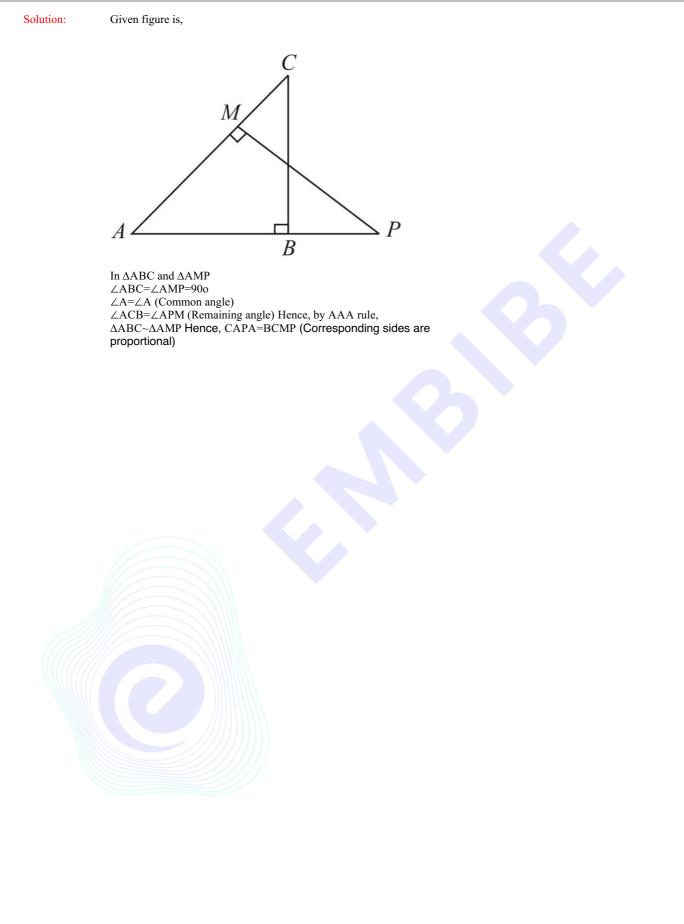


Chapter 6 Triangles











# **Exercise 6.4**

Q.1. Let  $\triangle ABC \sim \triangle DEF$  and their areas be 64 cm2 and 121cm2 respectively. If EF=15.4 cm, find BC.

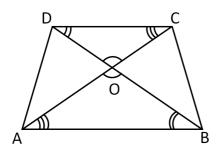
Solution: Given,  $\triangle ABC \sim \triangle DEF$ 

We have,

area( $\triangle$ ABC)area( $\triangle$ DEF)=ABDE2=BCEF2=ACDF2 Since EF=15.4, area $\triangle$ ABC=64, area $\triangle$ DEF=121. Hence, 64121=BC215.42  $\Rightarrow$ BC15.4=811  $\Rightarrow$ BC=8×15.411=8×1.4=11.2 cm. Thus, BC=11.2 cm.

Q.2. Diagonals of a trapezium ABCD with ABIDC intersect each other at the point O. If AB=2CD, find the ratio of the areas of triangles AOB and COD.

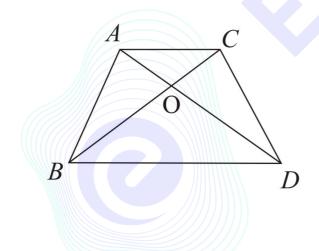
Solution:



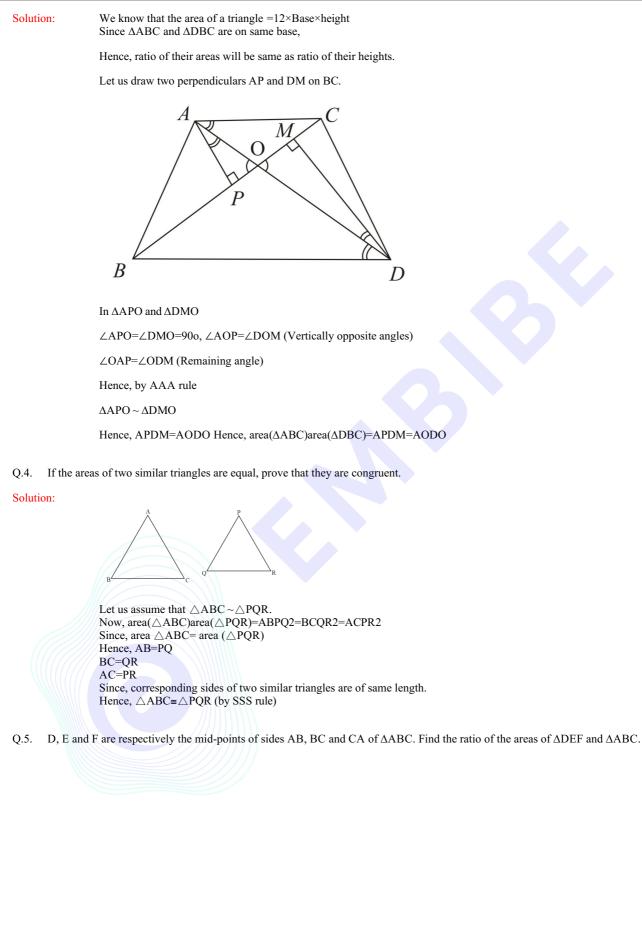
Since ABICD,

 $\angle OAB = \angle OCD$  (Alternate interior angles)  $\angle OBA = \angle ODC$  (Alternate interior angles)  $\angle AOB = \angle COD$  (Vertically opposite angles) Hence, by AAA rule,  $\triangle AOB \sim \triangle COD \Rightarrow area(\triangle AOB)area(\triangle COD) = ABCD2$  Since AB=2CD,  $area(\triangle AOB)area(\triangle COD) = 41=4:1$  Hence, the ratio of the areas of triangles AOB and COD is 4:1.

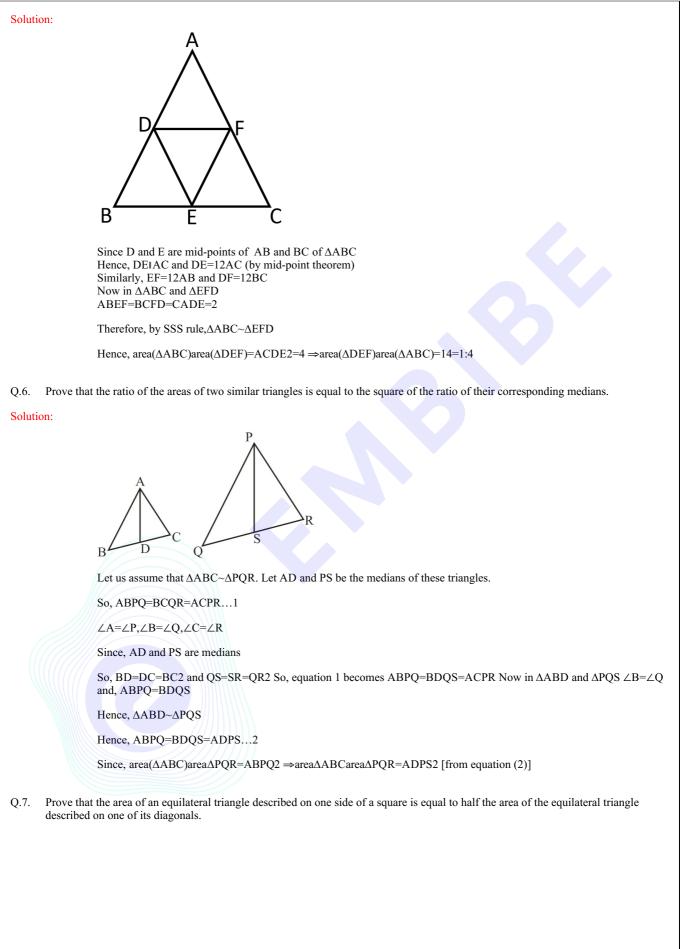
Q.3. In the figure, ABC and DBC are two triangles on the same base BC. If AD intersects BC at O, show that arABCarDBC=AODO.



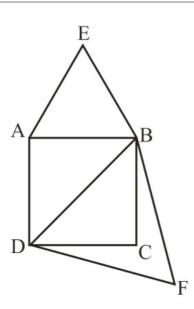












Let ABCD be a square of side a. Therefore, it's diagonal =2a.

Let  $\triangle ABE$  and  $\triangle DBF$  are two equilateral triangles. Hence, AB=AE=BE=a and DB=DF=BF=2a. We know that all angles of equilateral triangles are 60o.

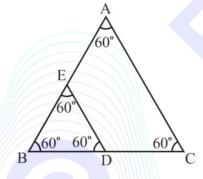
Hence, all equilateral triangles are similar to each other.

Hence, ratio of areas of these triangles will be equal to the square of the ratio between sides of these triangles.

area of  $\triangle ABE$  area of  $\triangle DBF$ =a2a2=12 Hence, area of  $\triangle ABE$ =12(area of  $\triangle DBF$ ).

Q.8. ABC and BDE are two equilateral triangles such that D is the midpoint of BC. Ratio of the areas of triangles ABC and BDE is 2:11:24:1

## Solution:



Since, all angle of equilateral triangles are 600, all equilateral triangles are similar to each other.

Therefore, ratio between areas of these triangles will be equal to the square of the ratio between sides of these triangles.

Let side of  $\triangle ABC=a$  Therefore, side of  $\triangle BDE=a2$  Hence, area $\triangle ABC$ area $\triangle BDE=aa22=41=4:1$ 

# 1:4

Q.9. Sides of two similar triangles are in the ratio 4:9. Areas of these triangles are in the ratio 2:34:981:1616:81

## Solution:

We know that,

If two triangles are similar to each other, the ratio between areas of these triangles will be equal to the square of the ratio between sides of these triangles.

Given that sides are in the ratio 4:9. Hence, ratio between areas of these triangles =492=1681=16:81.



## Exercise 6.5

Q.1. Sides of a triangle are given below. Determine if it is a right triangle. In case of a right triangle, write the length of its hypotenuse. 7 cm, 24 cm, 25 cm

Solution: Given that sides are 7 cm, 24 cm and 25 cm.

Squaring the lengths of these sides we get 49, 576 and 625.

Clearly, 49+576=625 or 72+242=252. The given triangle satisfies Pythagoras theorem. So, it is a right triangle. We know that the longest side in a right triangle is the hypotenuse. Hence, length of hypotenuse =25 cm.

Q.2. Sides of triangles are given below. Determine which of them are right triangles. In case of a right triangle, write the length of its hypotenuse.
3 cm, 8 cm, 6 cm

Solution:

Given that sides are 3 cm, 8 cm and 6 cm.

Here, 64≠36+9

Clearly, sum of squares of lengths of two sides is not equal to square of length of third side. Hence, given triangle is not satisfying Pythagoras theorem. So, it is not a right triangle.

Q.3. Sides of triangles are given below. Determine which of them are right triangles. In case of a right triangle, write the length of its hypotenuse.

50 cm, 80 cm, 100 cm

Solution: Given that sides are 50 cm, 80 cm and 100 cm.

Here, 10000≠6400+2500

Clearly, sum of squares of lengths of two sides is not equal to square of length of third side. Therefore, given triangle is not satisfying Pythagoras theorem. So, it is not a right triangle.

Q.4. The sides of a triangle are given below. Determine whether it is a right triangle. In case of a right triangle, write the length of its hypotenuse.

13 cm, 12 cm, 5 cm.

Given that sides are 13 cm, 12 cm and 5 cm.

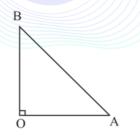
Squaring the lengths of these sides we may get 169, 144 and 25.

We know that, 144+25=169 or 122+52=132. So, by converse of Pythagoras theorem, it is a right triangle. As we know that the longest side in a right triangle is the hypotenuse. Hence, length of hypotenuse =13 cm.

Q.5. A guy wire attached to a vertical pole of height 18 m is 24 m long and has a stake attached to the other end. How far from the base of the pole should the stake be driven so that the wire will be taut?

Solution:

Solution:



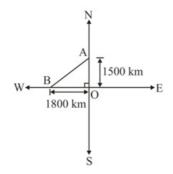
Let OB be the pole and AB be the wire. Therefore, by Pythagoras theorem we have: AB2=OB2+OA2  $\Rightarrow 242=182+OA2$   $\Rightarrow OA2=576-324$   $\Rightarrow OA=252=6\times6\times7=67$ Therefore, distance from base =67 m



Q.6. An aeroplane leaves an airport and flies due north at a speed of 1000 km per hour. At the same time, another aeroplane leaves the same airport and flies due west at a speed of 1200 km per hour. How far apart will be the two planes after 112 hours?

#### Solution:

Solution:



Distance traveled by the plane flying towards north in 112 hrs

=1,000×112=1,500 km

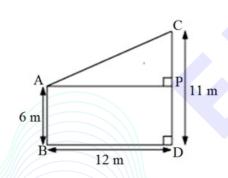
Distance traveled by the plane flying towards west in 112 hrs =1,200×112=1,800 km

Let these distances are represented by OA and OB respectively.

Now applying Pythagoras theorem

Distance between these planes after 112 hrs, AB=OA2+OB2=1,5002+1,8002=2250000+3240000=5490000=9×610000=30061 So, distance between these planes will be 30061 km. after 112 hrs.

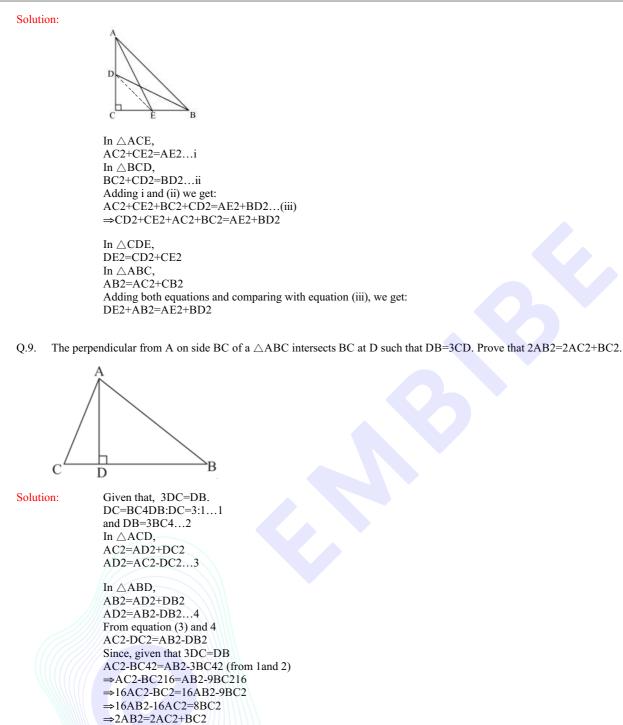
Q.7. Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between the feet of the poles is 12 m, find the distance between their tops.



Let CD and AB be the poles of height 11 m and 6 m. Therefore, CP=11-6=5 m From the figure we may observe that AP=12 m In  $\triangle$ APC, by applying Pythagoras theorem we get: AP2+PC2=AC2  $\Rightarrow$ 122+52=AC2  $\Rightarrow$ AC2=144+25=169  $\Rightarrow$ AC=13 Therefore, the distance between their tops =13 m.

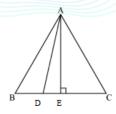
Q.8. D and E are points on the sides CA and CB respectively of a triangle ABC right-angled at C. Prove that AE2+BD2=AB2+DE2.





Q.10. In an equilateral triangle ABC, D is a point on side BC such that BD=13BC. Prove that 9AD2=7AB2.

Solution:



Let side of equilateral triangle be a and AE be the altitude of  $\Delta ABC$ 

So, BE=EC=BC2=a2

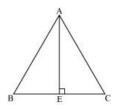
and, AE=a32 Given that BD=13BC=a3 So, DE=BE-BD=a2-a3=a6 Now, in  $\triangle$ ADE, by applying Pythagoras theorem AD2=AE2+DE2  $\Rightarrow$ AD2=a322+a62 =3a24+a236=28a236 or, 9AD2=7AB2

Q.11. In an equilateral triangle, prove that three times the square of one side is equal to four times the square of one of its altitudes.

# NCERT Mathematics





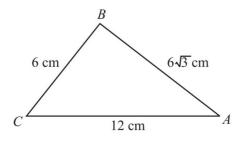


Let side of equilateral triangle be a. And AE be the altitude of  $\triangle ABC$ 

So, BE=EC=BC2=a2 Now in  $\triangle ABE$  by applying Pythagoras theorem AB2=AE2+BE2  $\Rightarrow$ a2=AE2+a22  $\Rightarrow AE2=a2-a24$  $\Rightarrow AE2=3a24 \Rightarrow 4AE2=3a2$  or,  $4AE2=3\times$  square of one side.

Q.12. In  $\triangle$ ABC, AB=63 cm, AC=12 cm and BC=6 cm. The angle B is 120o60o90o

# Solution:



Given that AB=63 cm, AC=12 cm and BC=6 cm

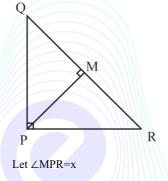
We may observe that

AB2=108, AC2=144 and BC2=36, AB2+BC2=AC2 Thus, the given  $\triangle$ ABC is satisfying Pythagoras theorem. Therefore, the triangle is a right angle triangle right-angled at B Therefore,  $\angle$ B=90°.

#### 450

Q.13. PQR is a triangle right-angled at P and M is a point on QR such that PMLQR. Show that PM2=QM.MR.

## Solution:



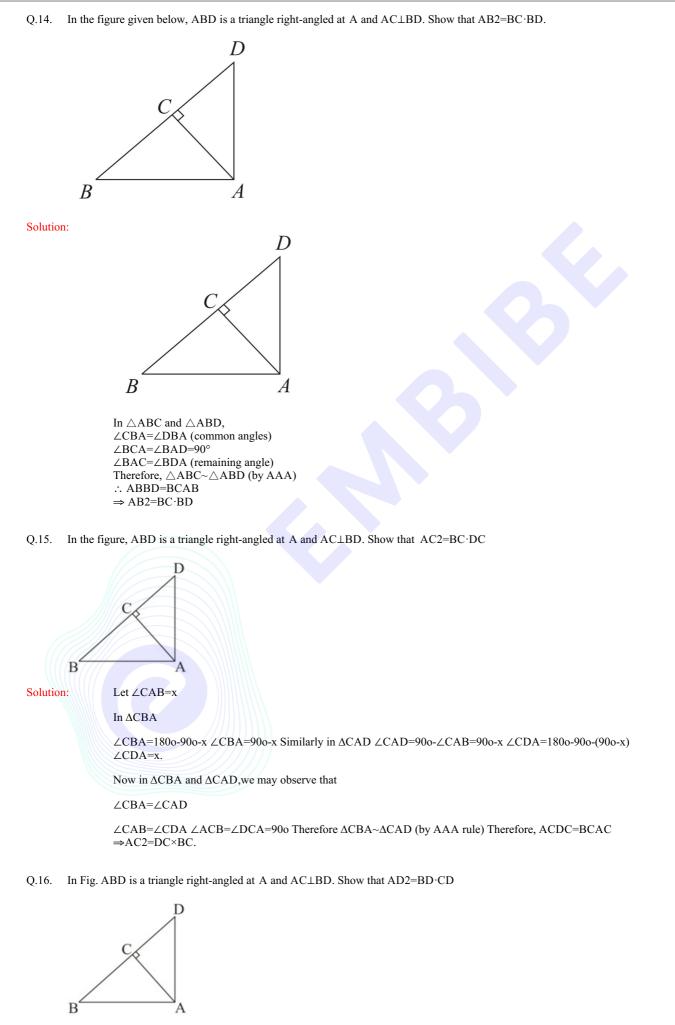
In  $\triangle$ MPR  $\angle$ MRP=1800-900-x  $\Rightarrow \angle$ MRP=900-x Similarly in  $\triangle$ MPQ  $\angle$ MPQ=900- $\angle$ MPR=900-x  $\angle$ MQP=1800-900-900-x  $\Rightarrow \angle$ MQP=x

Now in  $\Delta$ MPQ and  $\Delta$ MRP, we may observe that

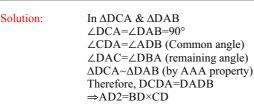
∠MPQ=∠MRP

 $\angle PMQ = \angle RMP \angle MQP = \angle MPR$  Hence, by AAA rule,  $\triangle MPQ \sim \triangle MRP$  Hence, QMPM=MPMR  $\Rightarrow PM2 = QM.MR$ 



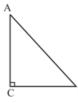






Q.17. ABC is an isosceles triangle right-angled at C. Prove that AB2=2AC2.

Solution:

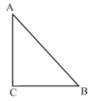


Given that  $\triangle ABC$  is an isosceles triangle.

Therefore, AC=CB Applying Pythagoras theorem in  $\triangle$ ABC ( i.e. right-angled at point C) AC2+CB2=AB2  $\Rightarrow$ 2AC2=AB2 (as AC=CB)

Q.18. ABC is an isosceles triangle with AC=BC. If AB2=2AC2, prove that ABC is a right triangle.

## Solution:



Given that AB2=2AC2

 $\Rightarrow$ AB2=AC2+AC2  $\Rightarrow$ AB2=AC2+BC2 (as AC=BC) Therefore, by converse of Pythagoras theorem, given triangle is a right-angled triangle.

Q.19. ABC is an equilateral triangle of side 2a. Find each of its altitudes.

Solution:

B D C

Let AD be the altitude in given equilateral  $\triangle ABC$ .

We know that altitude bisects the opposite side. So, BD=DC=a in  $\triangle$ ADB  $\angle$ ADB=900

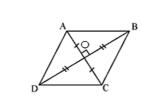
Now applying Pythagoras theorem

AD2+BD2=AB2

 $\Rightarrow$ AD2+a2=2a2  $\Rightarrow$ AD2+a2=4a2  $\Rightarrow$ AD2=3a2  $\Rightarrow$ AD=a3 Since in an equilateral triangle, all the altitudes are equal in length. So, length of each altitude will be 3a

Q.20. Prove that the sum of the squares of the sides of a rhombus is equal to the sum of the squares of its diagonals.

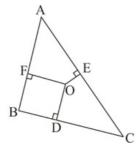




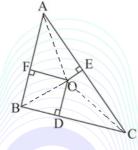
In  $\triangle AOB, \triangle BOC, \triangle COD, \triangle AOD$ Applying Pythagoras theorem AB2=AO2+OB2 BC2=BO2+OC2 CD2=CO2+OD2 AD2=AO2+OD2

Adding all these equations, AB2+BC2+CD2+AD2=2AO2+OB2+OC2+OD2 =2AC22+BD22+AC22+BD22 (diagonals bisect each other.) =2AC22+BD22 =AC2+BD2

Q.21. In Fig. 6.54, O is a point in the interior of a triangle ABC, OD⊥BC, OE⊥AC and OF⊥AB. Show that OA2+OB2+OC2-OD2-OE2-OF2=AF2+BD2+CE2,

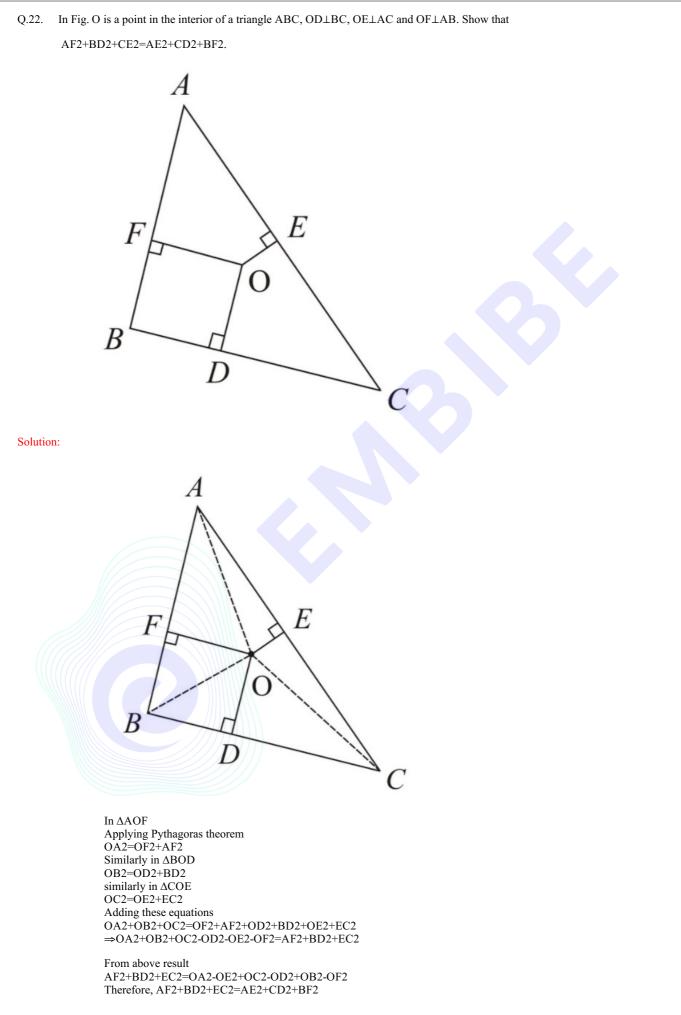


Solution:



In  $\triangle AOF$ Applying Pythagoras theorem OA2=OF2+AF2Similarly in  $\triangle BOD$  OB2=OD2+BD2similarly in  $\triangle COE$  OC2=OE2+EC2Adding these equations OA2+OB2+OC2=OF2+AF2+OD2+BD2+OE2+EC2 $\Rightarrow OA2+OB2+OC2-OD2-OE2-OF2=AF2+BD2+EC2$ 

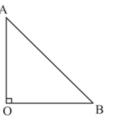






Q.23. A ladder 10 m long reaches a window 8 m above the ground. Find the distance of the foot of the ladder from base of the wall.

## Solution:



Let OA be the wall and AB be the ladder.

Therefore by Pythagoras theorem, AB2=OA2+BO2  $\Rightarrow 102=82+OB2$   $\Rightarrow 100=64+OB2$   $\Rightarrow OB2=36$  $\Rightarrow OB=6$ 

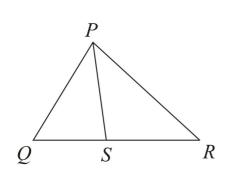
Therefore, distance of foot of ladder from of the wall =6 m



## **Exercise 6.6**

Q.1. In the given figure, PS is the bisector of  $\angle$ QPR of  $\triangle$ PQR. Prove that QSSR=PQPR.

7



Solution:

Given that, PS is angle bisector of  $\angle QPR$ .

Q

P

Construct a line RT parallel to SP which meets QP produced at T.  $\angle$ QPS= $\angle$ SPR .....(1)  $\angle$ SPR= $\angle$ PRT (As PS||TR, alternate interior angles) .....(2)  $\angle$ QPS= $\angle$ QTR (As PS||TR, corresponding angles) .....(3) Using these equations, we may find  $\angle$ PRT= $\angle$ QTR from (2) and (3) So, PT=PR (Since  $\triangle$ PTR is isosceles triangle)

R

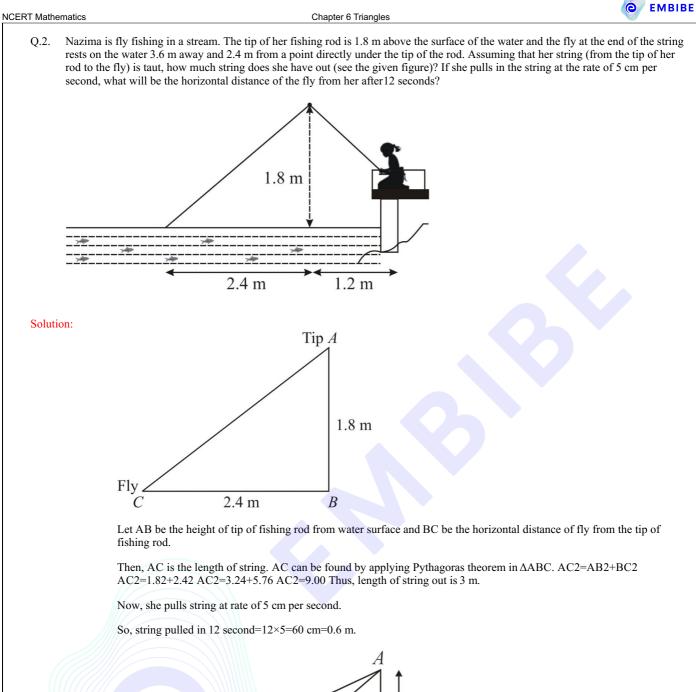
Now in  $\triangle QPS$  and  $\triangle QTR$ ,  $\angle QSP = \angle QRT$  (As PS ||TR)

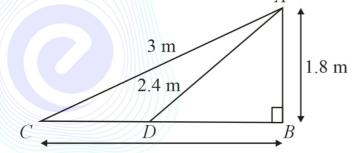
S

 $\angle QPS = \angle QTR$  (As PS || TR)

 $\angle Q$  is common.  $\triangle QPS \sim \triangle QTR$  $\Rightarrow QSSR = QPPT \Rightarrow QSSR = PQPR$ 

(by AAA property) So, QRQS=QTQP  $\Rightarrow$  QRQS-1=QTQP-1  $\Rightarrow$  SRQS=PTQP

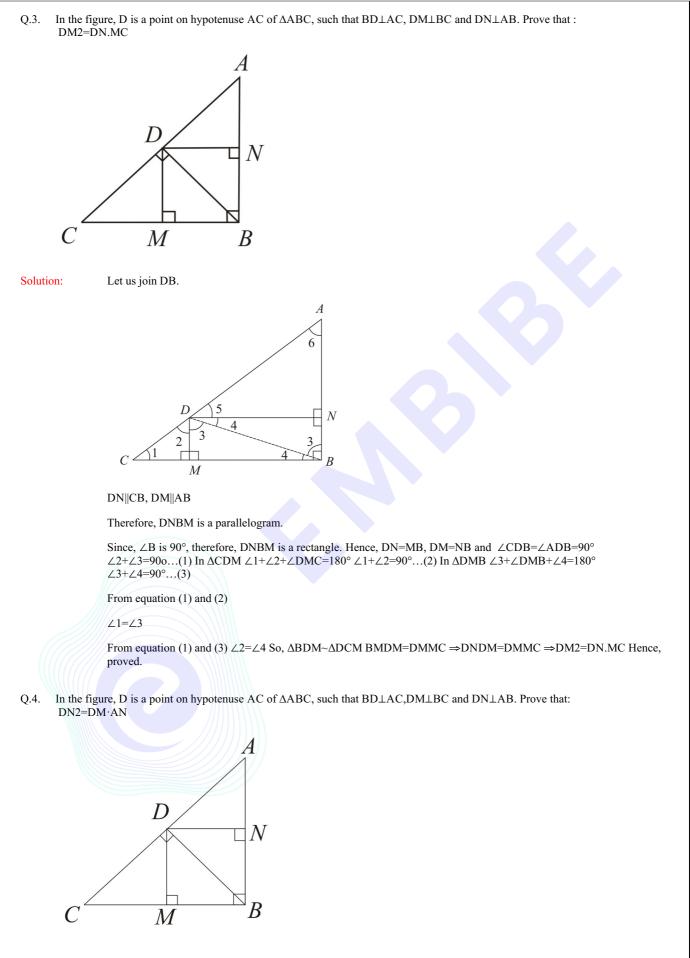




After 12 seconds, let us assume the fly to be at point D.

Length of string out after 12 second is AD. AD=AC- string pulled by Nazima in 12 second =3.00-0.6 =2.4 m In  $\triangle$ ADB, AB2+BD2=AD2  $\Rightarrow$ 1.82+BD2=2.42  $\Rightarrow$ BD2=5.76-3.24=2.52  $\Rightarrow$ BD=1.587 m Horizontal distance of fly =BD+1.2 =1.587+1.2 =2.787 =2.79 m

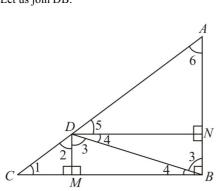




Solution:

Let us join DB.





DN||CB, DM||AB

Therefore, DNBM is a parallelogram.

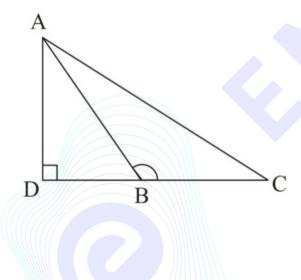
Since,  $\angle B$  is 90°. Therefore, DNBM is a rectangle. So, DN=MB, DM=NB and  $\angle CDB=\angle ADB=90^{\circ} \angle 4+\angle 5=900...(1)$ In  $\triangle ADN \angle 5+\angle 6=90^{\circ}...(2)$ 

From equation (1) and (2)

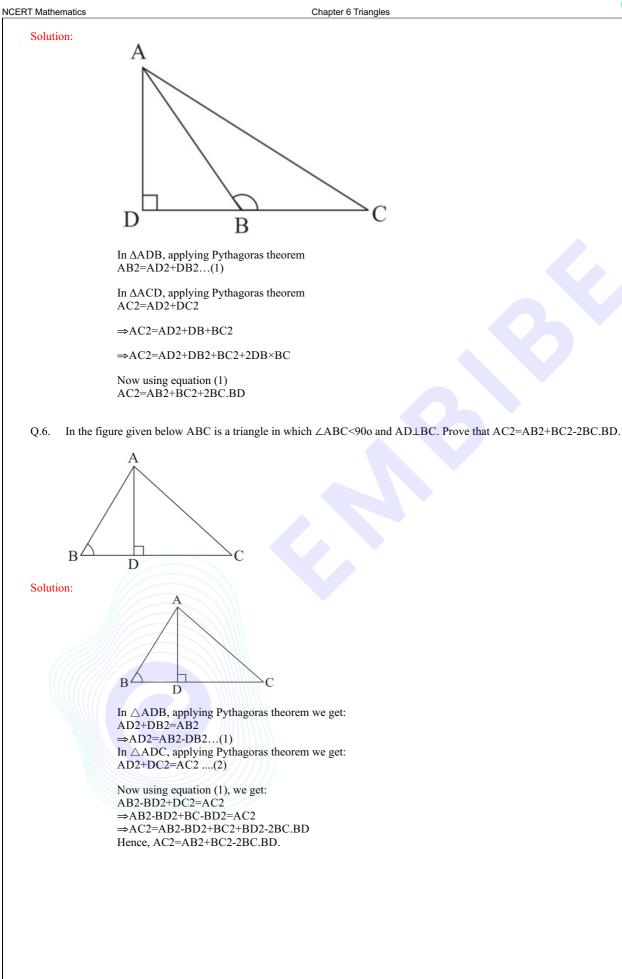
∠4=∠6

and  $\angle DNA = \angle DNB = 90^{\circ}$  So,  $\triangle ADN \sim \triangle BDN DNBN = ANDN \Rightarrow DNDM = ANDN (As BN=DM) \Rightarrow DN2 = DM \times AN$  Hence, proved.

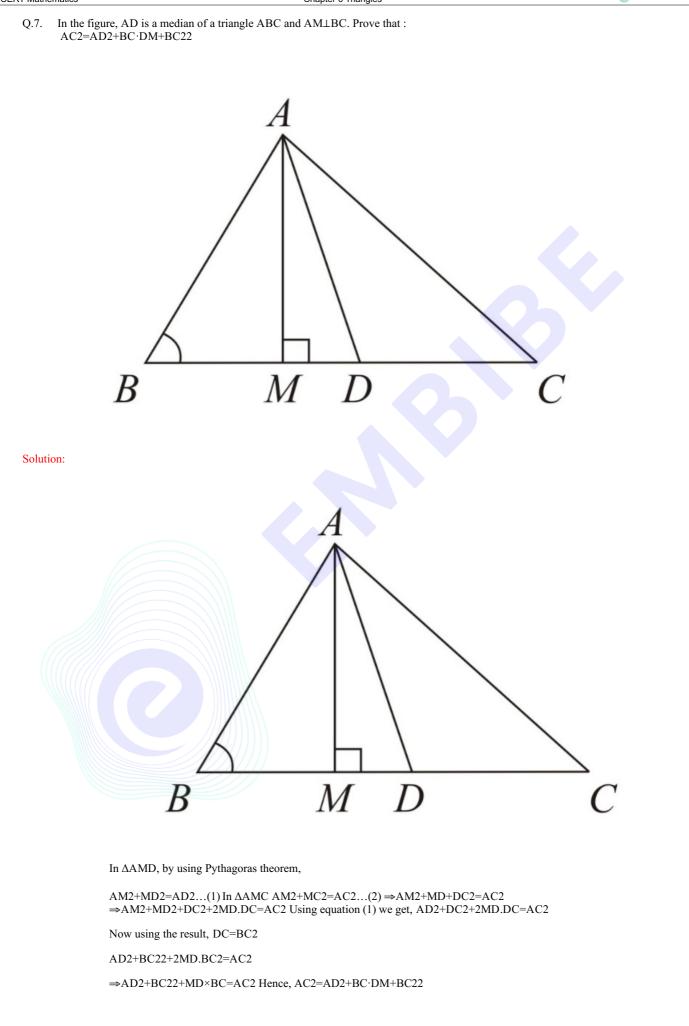
Q.5. ABC is a triangle in which ∠ABC>900 and AD⊥CB produced. Prove that AC2=AB2+BC2+2BC·BD.



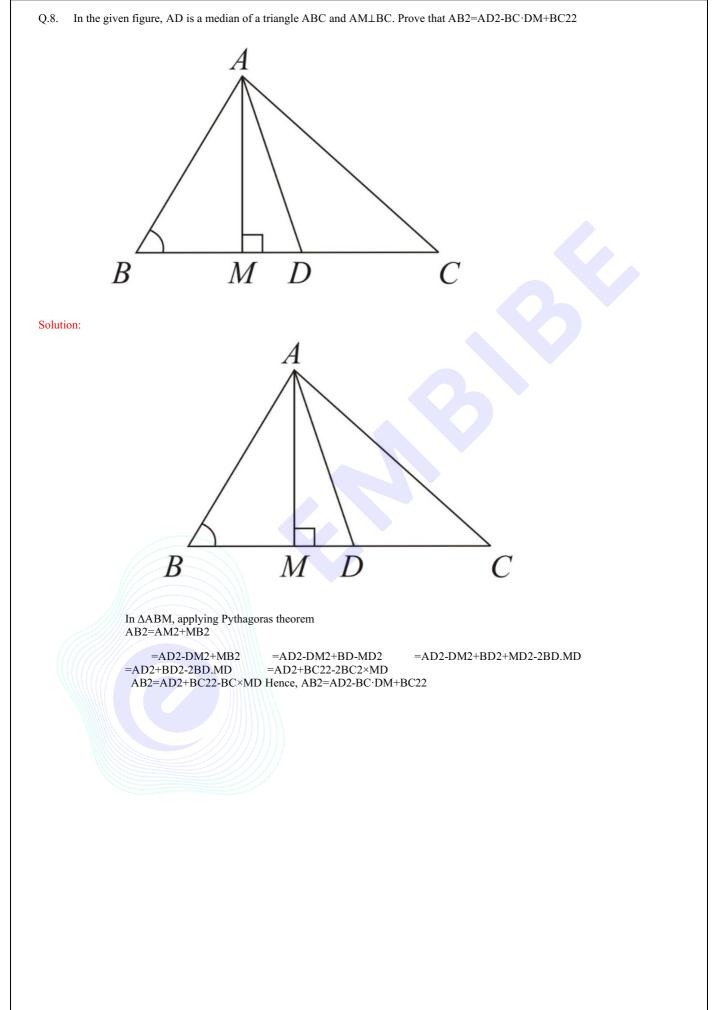




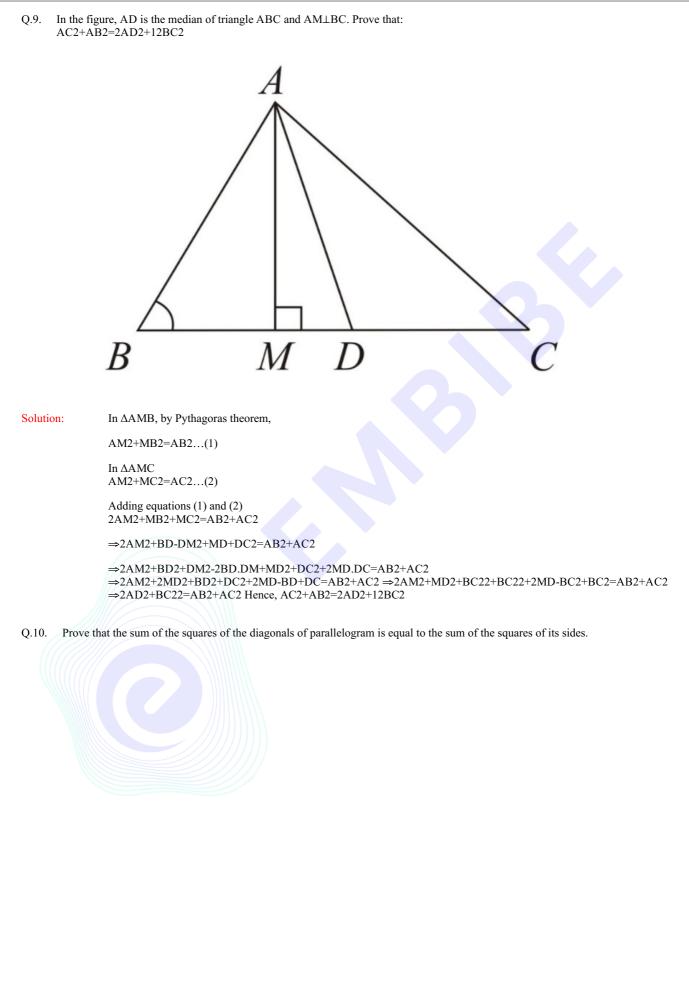




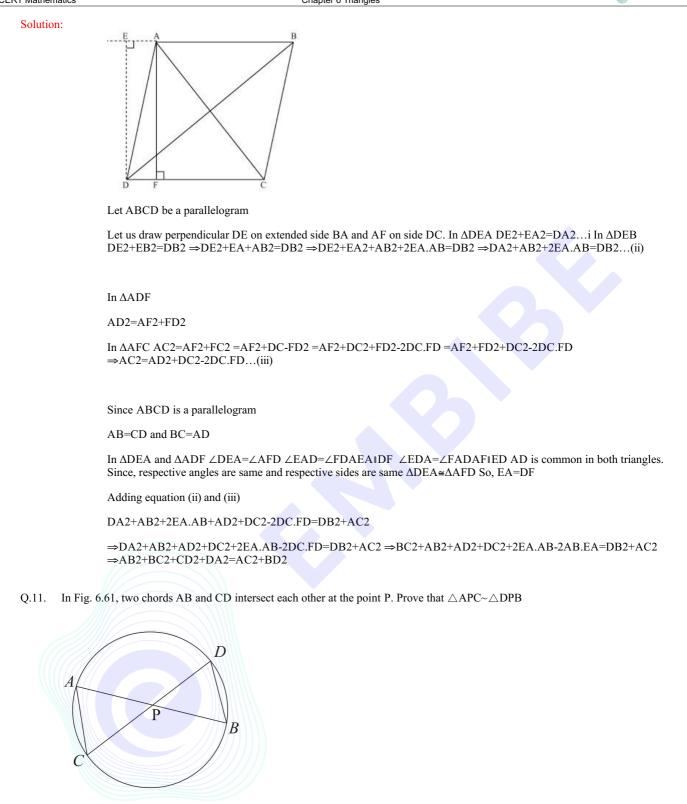




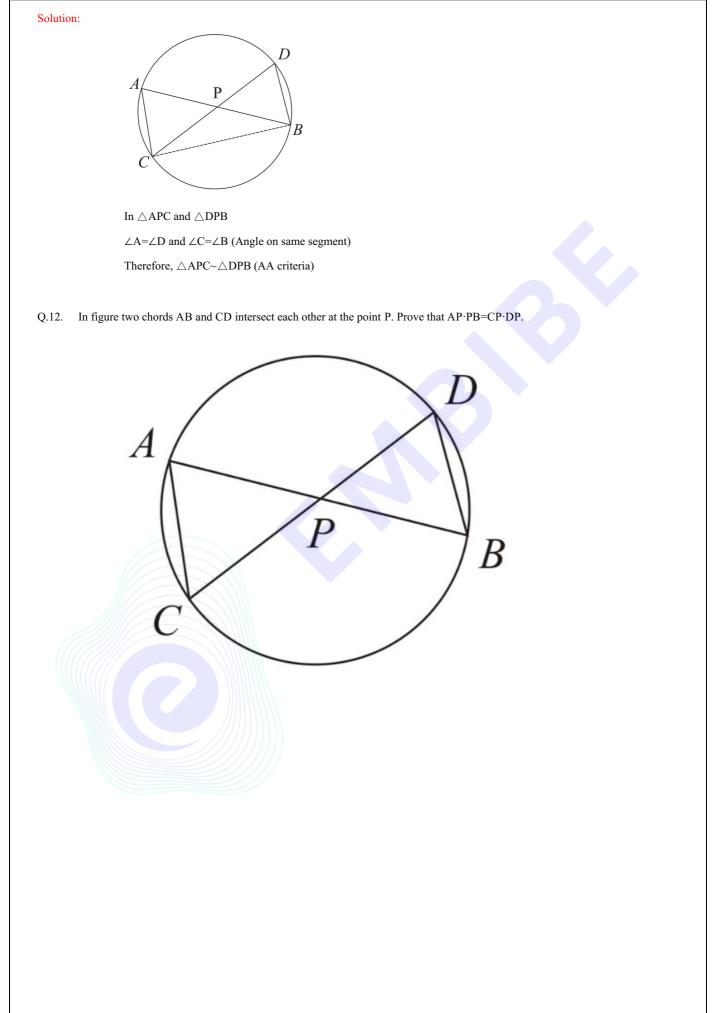




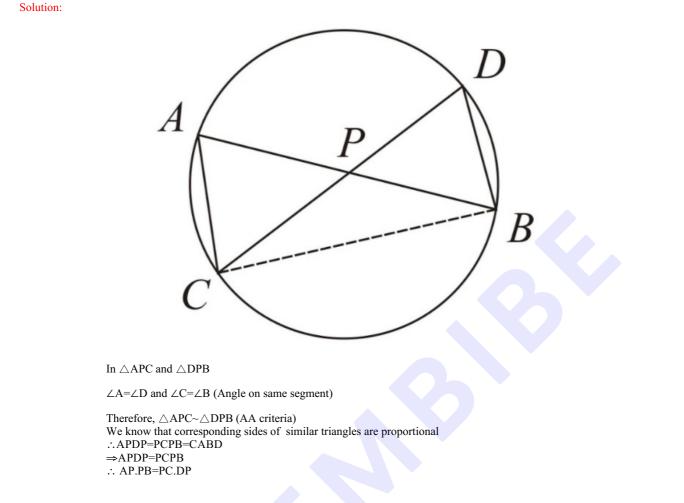




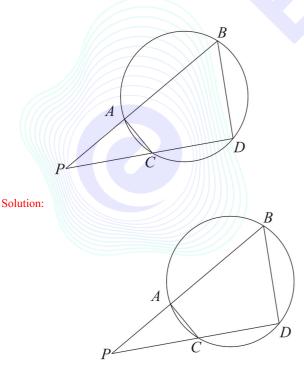








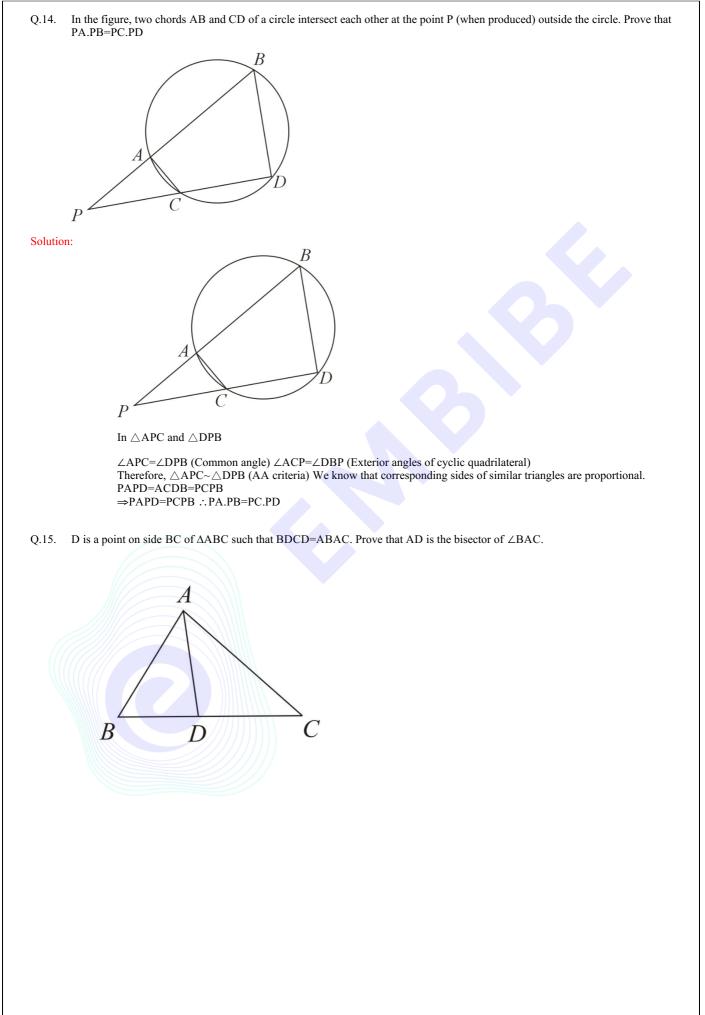
Q.13. In the figure, two chords AB and CD of a circle intersect each other at the point P (when produced) outside the circle. Prove that  $\triangle PAC \sim \triangle PDB$ .



In  $\triangle PAC$  and  $\triangle PDB$ 

 $\angle APC = \angle DPB$  (Common angle)  $\angle ACP = \angle DBP$  (Exterior angle of a cyclic quadrilateral is equal to the opposite interior angle.) Therefore,  $\triangle PAC \sim \triangle PDB$  (AA criteria)





Solution:



Construct a line CE parallel to DA which meets BA produced at E.

Therefore,  $\angle BAD = \angle BEC$  (Corresponding angles).....(1)  $\angle DAC = \angle ACE$  (Alternate angles).....(2) In  $\triangle DBA$  and  $\triangle CBE$ , BDCD=ABAC (Given) .....(3) BDCD=BAAE (Basic proportionality theorem) .....(4) From (3) and (4), AE=AC Therefore,  $\angle ACE = \angle BEC$ .....(5) So, from (1), (2) and (5)  $\Rightarrow \angle BAD = \angle DAC$  Therefore, AD is angle bisector of  $\angle BAC$ .

