EMBIBE

# JEE Main Exam 2022 - Session 2

# 27 Jul 2022 - Shift 1 (Memory-Based Questions)

# **Section A: Physics**

Q.1. A *DC* current of 4 A and *AC* current of peak value 4 A passes through 3 Ω and 2 Ω resistors respectively. Find the ratio of heat generated

A) 3:1

- B) 3:2
- C) 3:4
- D) 1:1

Answer: 3:1

Solution: Heat in DC is given by,

$$H_{DC} = \left(i^2 R\right) t = 4^2 \times 3 \times t = 48t$$

Heat in AC is given by,

 $H_{AC} = (V_{\rm rms} I_{\rm rms} \cos \phi) t$ 

Since, only resistance is present  $Z = R \Rightarrow V_{rms} = I_{rms}R$  and  $\cos \phi = 1$ 

$$\Rightarrow H_{AC} = (I_{\rm rms})^2 R \cos \phi t = I_{\rm rms}^2 R t = \left(\frac{4}{\sqrt{2}}\right)^2 \times 2 \times t$$

 $\Rightarrow H_{AC} = 16t$ 

Therefore, the ratio  $\frac{H_DC}{H_AC} = \frac{3}{1}$ 

- Q.2. In a station, the TV transmission tower is of height 100 m. In order to triple the coverage range, the height should be increased to
- A) 200 m
- B) 300 m
- C) 600 m
- D) 900 m

Answer: 900 m

Solution: Range of signal from an antenna is given by,

 $r=\sqrt{2hR}$ 

Therefore,

$$\frac{h_2}{h_1} = \left(\frac{r_2}{r_1}\right)^2$$
$$\Rightarrow h_2 = 3^2 \times 100 = 900 \text{ m}$$

Q.3. Two bar magnets oscillate in earth magnetic field with the time period of 3 s and 4 s. If ratio of moment of inertia is 3:2, then the ratio of the magnetic moment is

A) 4:1

B) 8:3

- C) 27:16
- D) 2:1



### Answer: 8:3

Solution: The time period of bar magnets is given by,

$$T = 2\pi \sqrt{\frac{I}{MB}} \Rightarrow M \propto \frac{I}{T^2}$$
$$\Rightarrow \frac{M_1}{M_2} = \frac{I_1}{I_2} \times \left(\frac{T_2}{T_1}\right)^2$$
$$\Rightarrow \frac{M_1}{M_2} = \frac{3}{2} \times \left(\frac{4}{3}\right)^2 = \frac{8}{3}$$

Q.4. Maximum error in the measurement of force is 5% and that in measurement of length is 5%. Maximum possible error in measurement of torque is (angle between force and position vector is known to be accurate)

A) 10%

**B)** 20%

C) 15%

**D)** 5%

Answer: 10%

Solution: Torque of a force is given by,

 $\overrightarrow{ au} = \overrightarrow{r} imes \overrightarrow{F}$ 

 $\Rightarrow \tau = rF\sin\theta$ 

As the angle is known to be accurate,

$$\Rightarrow \quad \frac{\Delta \tau}{\tau} \times 100 = \left[\frac{\Delta r}{r} + \frac{\Delta F}{F}\right] \times 100$$

Therefore, percentage error in  $\tau = 5\% + 5\%$ 

= 10%

Q.5. A bag is dropped on a conveyor belt with coefficient of friction  $\mu$ . The belt keeps on moving with constant speed v. The time it takes for relative motion between bag and belt to stop is

A)  $\frac{v}{g}$ B)  $\frac{v}{2\mu g}$ C)  $\frac{v}{2\mu g}$ 

D)  $\frac{g}{v}$ 

Answer:  $\frac{v}{\mu g}$ 

Solution: The acceleration of the bag when it is dropped on the conveyor belt will be,

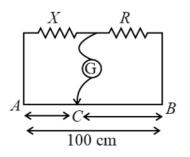
 $a = \mu g.$ 

The relative velocity between the bag and the conveyor will stop when the bag will achieve velocity of v. Using the equation of motion,

 $v = u + at \Rightarrow v = \mu gt$  $\Rightarrow t = \frac{v}{\mu g}$ 



Q.6. In the shown meter bridge the null point C is obtained 30 cm away from point A. If  $R = 5.6 \text{ k}\Omega$ , then the value of resistance of resistor X is



A) 1.6 kΩ

B) 2.4 kΩ

C) 4.8 kΩ

D) 5.8 kΩ

Answer:  $2.4 \text{ k}\Omega$ 

Solution: For the null point of the potentiometer,

$$\frac{X}{R} = \frac{l}{L-l}$$

$$\Rightarrow \quad \frac{X}{5.6} = \frac{30}{70}$$

$$\Rightarrow \quad X = 3 \times 0.8 = 2.4 \text{ k}\Omega$$

Q.7. Waves of intensity *I* and 4*I* with same frequency interfere at two points *A* and *B* such that at *A*, phase difference between the two is  $\frac{\pi}{2}$ , while at *B* it is  $\frac{\pi}{3}$ . The difference between net intensities at two points is equal to

A) I

B) 7*I* 

C) 3I

D) 21

Answer: 21

Solution: The intensity of the two waves interfering at a point having phase difference  $\phi$  is given by,

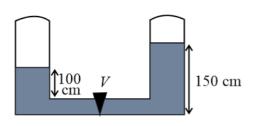
$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$$

$$\Rightarrow I_A = I + 4I + 2\sqrt{4I^2} \times \cos\frac{\pi}{2} = 5I$$

and

$$\begin{split} I_B = I + 4I + 2\sqrt{4I^2} \times \cos\frac{\pi}{3} &= 5I + 2I = 7I \\ \Delta I = |I_A - I_B| &= 2I \end{split}$$

Q.8. The cylinders shown have an area of cross-section of  $16 \text{ cm}^2$ . In one cylinder the water is raised upto 100 cm while in other the water is raised upto 150 cm. After opening of the valve *V*, the work done by gravity when levels set is equal to



A) 5 J



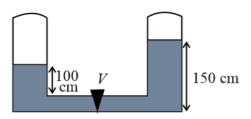
B) 1 JC) 17.25 J

D) 25 J

### Answer:

1 J

Solution:



Initially, the centre of mass of the right column will be at height of 75 cm and the centre of mass of the left column will be at 50 cm. After opening of the valve both columns will have height of 125 cm and their centre of mass will be at height  $\frac{125}{2}$  cm. Therefore,

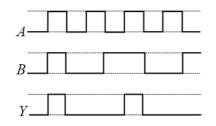
$$W = -\Delta U = -\left[(m_1 + m_2)g rac{h_1 + h_2}{4} - m_1g rac{h_1}{2} - m_2g rac{h_2}{2}
ight]$$

Now,  $m_1 = 
ho A h_1$  and  $m_2 = 
ho A h_2$ 

Putting  $\rho = 1000 \text{ kg m}^{-3}$ ,  $g = 10 \text{ m s}^{-2}$ ,  $h_1 = 100 \text{ cm}$ ,  $h_2 = 150 \text{ cm}$  and  $A = 16 \times 10^{-4} \text{ m}^2$ , we get,

 $W = 1~{\rm J}$ 

Q.9. The shown signals *A* and *B* are used as input to logic gate with *Y* as its output as shown. Identify the logic gate.



A) AND

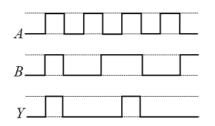
B) OR

C) NOR

D) NAND

Answer: AND

Solution:



From the above diagram, we can see,

if A = 0, B = 0, then Y = 0.

if A = 1, B = 0, then Y = 0.

if A = 0, B = 1, then Y = 0.

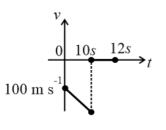
if A = 1, B = 1, then Y = 1.

Clearly, the logic gate is a AND gate.

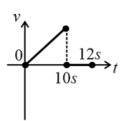


Q.10. A bullet is shot vertically downwards at  $100 \text{ m s}^{-1}$  and strikes ground below after 10 s then it stays at rest there for further 2 s. The appropriate v - t graph will be,

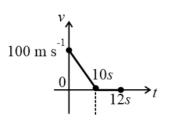
A)



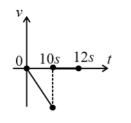
B)



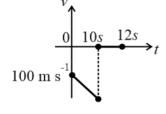








Answer:





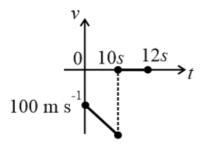
Solution: Let velocity of ball at any time is v during the downward motion, then we can write,

v = u + gt $\Rightarrow v = -100 - 10t$ 

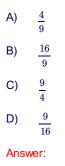
Velocity at the end of t = 10 s,  $v = -200 \text{ m s}^{-1}$ 

Once bullet strikes ground, it is at rest and hence velocity for that duration is  $0 \ {\rm m \ s^{-1}}.$ 

Hence, upto 10 s velocity of the ball will decrease and the graph will be straight line with negative slope and from 10 s onwards, it will be a horizontal line on *X*-axis.



Q.11. Two satellites A and B have mass ratio 1:3 and their distance from the centre of earth are 3r and 4r respectively. Their total energies are in the ratio. (neglecting self energy)

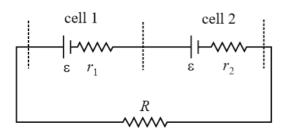


 $\frac{4}{9}$ 

Solution: Total energy of the satellite at r distance from the centre of the earth is given by,  $TE = \frac{-G_M m}{2r}$ .

Now, we can write, 
$$\Rightarrow \frac{TE_A}{TE_B} = \frac{\frac{-G_M(m)}{2(3r)}}{\frac{-G_M(3m)}{2(4r)}} = \frac{4}{9}$$

Q.12. Two cells, cell 1 and cell 2 are in series across the resistance *R*. Find the value of *R* such that potential difference across cell 1 is zero.



A)  $r_1 - r_2$ 

- B)  $r_1 + r_2$
- C)  $(r_1 r_2)$
- 1
- D)  $r_1+r_2$



Answer:  $r_1 - r_2$ 

Solution: Current through the wire will be,

$$I\!=\!\frac{2\varepsilon}{R\!+\!r_1\!+\!r_2}.$$

Now potential difference across cell 1 will be,  $arepsilon - Ir_1 = 0$ 

$$\Rightarrow \varepsilon = \frac{2\varepsilon}{R + r_1 + r_2} \times r_1$$
$$\Rightarrow R + r_1 + r_2 = 2r_1$$
$$\Rightarrow R = r_1 - r_2$$

Q.13. Two point charges each of magnitude Q are kept fixed at a distance 2d from each other. A third charge q is kept at middle of the two charges and is displaced a little along the line joining the two charges. The time period of oscillations is (Take mass  $m_q = m$ )

A) 
$$2\pi\sqrt{\frac{\pi\epsilon_0 m d^3}{Qq}}$$
  
B)  $\pi\sqrt{\frac{\pi\epsilon_0 m d^3}{Qq}}$ 

C) 
$$2\pi \sqrt{\frac{Qq}{Qq}}$$

D) 
$$2\sqrt{\frac{\pi\epsilon_0 m d^3}{Qq}}$$

Answer: 
$$2\pi\sqrt{\frac{\pi\epsilon_0 m d^3}{Qq}}$$



Solution:

$$Q \xrightarrow{F_2} \xrightarrow{F_1} Q$$

$$1 \xrightarrow{(q,m)} 2$$

Let the charged particle be displaced slightly towards right by distance  $x \, (x \ll d)$ .

$$(Q \ at \ A, \ q): F_1 = rac{1}{4\piarepsilon_0} rac{Qq}{(d+x)^2},$$
 towards right

 $(Q ext{ at } B, \ q): \ F_2 = rac{1}{4\piarepsilon_0} rac{Qq}{(d-x)^2}, ext{ towards left}$ 

$$\vec{F}_{net} = \vec{F}_1 + \vec{F}_2, \text{ will bring it towards } O.\vec{F}_{net} = \frac{1}{4\pi\epsilon_0} \left[ \frac{1}{(d+x)^2} - \frac{1}{(d-x)^2} \right] \hat{i}$$

$$=\frac{-Qq}{4\pi\epsilon_0}\left[\frac{4xd}{\left(d^2-x^2\right)^2}\right]\hat{i}$$

Since  $x \ll d$ ,  $x^2$  is negligible.

$$\overrightarrow{F}_{net} = -\left(rac{Qq}{\pi\epsilon_0 d^3}
ight) imes x \hat{i}$$

Clearly, direction of the force is opposite to the displacement &  $F \propto x$ , hence it is a SHM.

Acceleration of charged particle is given as,

$$a = \frac{F}{m} = -\frac{Qq}{\pi\epsilon_0 m d^3} x \quad \dots (1)$$

and we know that,

$$a = -\omega^2 x \quad \dots (2)$$

Comparing (1) and (2), we get

$$\omega = \sqrt{\frac{Qq}{\pi\epsilon_0 m d^3}}$$

Hence, time period,  $T=\frac{2\pi}{\omega}=2\pi\sqrt{\frac{\pi\epsilon_{0}md^{3}}{Qq}}$ 

Q.14. Two rods, rod 1 and rod 2 are connected in series with each other in between two reservoirs maintained at 450 °C and 0 °C as shown. If  $\frac{k_1}{k_2} = 9$ ,  $\frac{l_1}{l_2} = 2$  and  $\frac{A_1}{A_2} = 2$ , then temperature of point *C* is (*k* is thermal conductance)

$$450^{\circ}C \xrightarrow{C} \underbrace{k_1, l_1, A_1}^{C} \underbrace{k_2, l_2, A_2}^{O^{\circ}C} \underbrace{0^{\circ}C}$$

A) 350 °C

- **B)** 45 °C
- **C)** 400 °C
- **D)** 405 °C

Answer: 405 °C



Solution: Let temperature at the point C is T. In series connection, heat current will be same through both the wires. Then,

$$\frac{k_1 A_1 (450^\circ - T)}{l_1} = \frac{k_2 A_2 (T - 0^\circ)}{l_2}$$
$$\Rightarrow \left(\frac{k_1}{k_2}\right) \left(\frac{A_1}{A_2}\right) (450^\circ - T) = T \left(\frac{l_1}{l_2}\right)$$
$$\Rightarrow 4050 - 9T = T$$
$$\Rightarrow T = \frac{4050}{10} = 405 \ ^\circ C$$

Q.15. A radioactive substance takes 30 years to reduce to  $\left(\frac{1}{16}\right)^{th}$  of its initial concentration. Find half life of the substance(in years).

A) 7.5

- **B**) 15
- **C**) 5
- D) 7

Answer: 7.5

Solution:

As we know,  $N=N_0 {\left(rac{1}{2}
ight)}^{rac{t}{t}} .$ 

Given, 
$$t = 30$$
 years for  $\frac{N}{N_0} = \frac{1}{16}$ .

Therefore,

$$\frac{30}{t_{1}}$$

$$\frac{1}{16} = \left(\frac{1}{2}\right)^{\frac{1}{2}}$$

$$\frac{30}{t_{1}}$$

$$\Rightarrow \left(\frac{1}{2}\right)^{4} = \left(\frac{1}{2}\right)^{\frac{1}{2}}$$

$$\Rightarrow 4 = \frac{30}{t_{1}}$$

$$\Rightarrow t_{\frac{1}{2}} = 7.5 \text{ years}$$



# **Section B: Chemistry**

- Q.16. The elevation in boiling point of a 2% aqueous solution of nonvolatile solute A is equal to the boiling point of 3% aqueous solution of non volatile solute B. Find the relation between their molecular weight. (Consider both solutes are non electrolytes.)
- A)  $M_A = 4M_B$
- B)  $M_B = 4M_A$
- C)  $3M_A = 2M_B$
- D)  $3M_B = 2M_A$

Answer:  $3M_A = 2M_B$ 

Solution:  $(\Delta T_b)_A = (\Delta T_b)_B$ 

 $\mathbf{k}_b\mathbf{m}_A = \mathbf{k}_b\mathbf{m}_B$ 

$$\begin{bmatrix} (W_A) \\ M_A \times W_{solvent} \end{bmatrix} = \begin{bmatrix} W_B \\ M_B \times W_{solvent} \end{bmatrix}$$
$$\frac{2}{M_A \times 98} = \frac{3}{M_B \times 97}$$

$$2M_B = 3M_A$$

- Q.17. Find out the solubility product of  $\operatorname{CaF}_2$  if solubility of  $\operatorname{CaF}_2$  is 2.34 g/100 mL.
- A)  $0.108 \, (mol/L)^3$
- B)  $0.072 \, (mol / L)^3$
- C)  $0.036 \, (mol/L)^3$
- D)  $0.032 \, (mol/L)^3$
- Answer:  $0.108 (mol/L)^3$

Solution:  $W_B = 2.34 \mathrm{g}$ 

 $\rm M_B\,{=}\,40+19+19=78~g/\,mol$ 

$$\begin{split} &\operatorname{CaF}_2(s) \Leftrightarrow \frac{\operatorname{Ca}_s^{2+}(\mathrm{aq}) + \frac{2F^-}{2s}(\mathrm{aq})} \\ &\operatorname{(Solubility)} \to \text{"Molarity"} \\ &\operatorname{k_{SP}} = s \times (2s)^2 \\ &= 4s^3 \\ &\operatorname{M} = \frac{2.34}{78} \times \frac{1000}{100} = 0.3 \mathrm{M} \end{split}$$

$$4s^3 = 4 \times (0.3)^3$$

- $= 4 \times 27 \times 10^{-3}$
- $=108 imes10^{-3}$
- $= 0.108 (mol/L)^3$
- Q.18. Assertion:  $SO_2$  is adsorbed more easily than  $CH_4$ .

Reason: Molar mass of  $SO_2$  is greater than  $CH_4$  and  $SO_2$  has a non-zero dipole moment.

- A) Both assertion and reason are correct and reason is correct explanation of assertion
- B) Both assertion and reason are correct and reason is not correct explanation of assertion
- C) Assertion is correct but reason is incorrect
- D) Assertion is incorrect but reason is correct



### Answer: Both assertion and reason are correct and reason is correct explanation of assertion

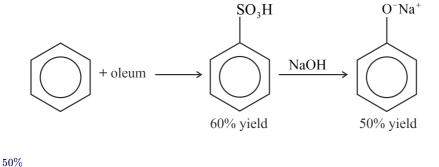
#### Solution: Lesser the value of critical temperature of gases lesser will be the extent of adsorption.

Gas	SO <sub>2</sub>	CH <sub>4</sub>
Critical temperature/K	630	190

The critical temperature depends on the strength of the intermolecular interactions that hold a substance together as a liquid.

 $SO_2$  has stronger intermolecular force of attractions than  $CH_4$ , due to the more molar mass and non-zero dipole moment.

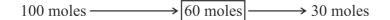
#### Q.19. The percentage yield of the complete reaction is:



- A) 50%
- **B)** 60%
- **C)** 30%
- D) 100%

#### Answer: 30%

Solution: Given that 60% yield in the first step, i.e, 100 moles of reactant gives 60 moles of the product. In the second step 50% yield is given, hence, 60 moles of benzene sulphonic acid gives 30 moles of phenoxide.



% yield = 30%

Q.20. Match List-I with List-II.

	List 1 (Polymer)		List 2 (Commercial name)
(A)	Phenol formaldehyde resin	(1)	Glyptal
<b>(</b> B)	Copolymer of 1, 3-butadiene and styrene	(2)	Novolac
(C)	Polymer of glycol and phthalic acid	(3)	Buna-S
(D)	Polymer of glycol and terephthalic acid	(4)	Dacron

- A) (A)-(1), (B)-(3), (C)-(2), (D)-(4)
- B) (A)-(2), (B)-(3), (C)-(1), (D)-(4)
- C) (A)-(4), (B)-(2), (C)-(3), (D)-(1)
- D) (A)-(3), (B)-(4), (C)-(2), (D)-(1)
- Answer: (A)-(2), (B)-(3), (C)-(1), (D)-(4)

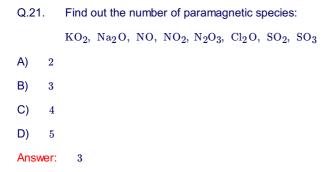
Solution: Novolacs are phenol-formaldehyde resins with a formaldehyde to phenol molar ratio of less than one.

The rubber obtained is also called Styrene butadiene rubber (SBR). In Buna-S, Bu stands for butadiene and, Na for sodium and S for styrene. It is vulcanised with sulfur. The rubber is slightly inferior to natural rubber in its physical properties.

Glyptal- a polyester is formed by ethylene glycol and phthalic acid by step-growth polymerization.

Dacron obtained by condensation polymerisation of ethylene glycol and terephthalic acid at 420 - 460 K using zinc acetate and antimony oxide as catalyst.





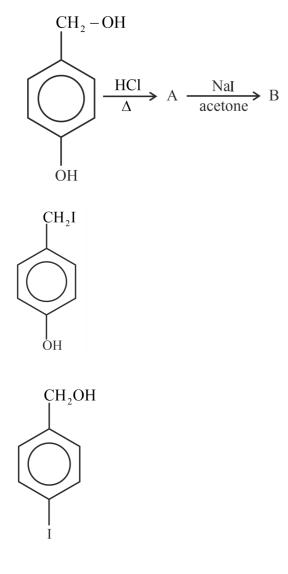
Solution: A molecule with odd electrons have one or more unpaired electrons. Molecules with unpaired electrons are para-magnetic. If all electrons are paired, then molecule is diamagnetic. KO<sub>2</sub>, NO and NO<sub>2</sub> are paramgnetic substances.

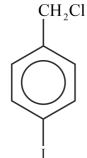


A)

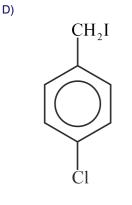
B)

C)





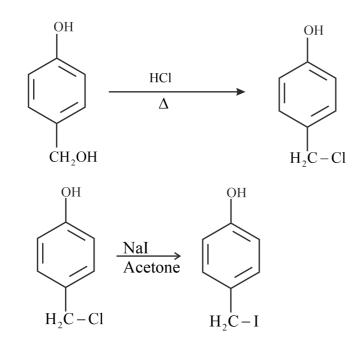




Answer:

CH<sub>2</sub>I





Q.23. In the titration of  $\rm KMnO_4$  with oxalic acid in acidic medium, the change in oxidation number of carbon per molecule of oxalic acid is

A) 4

- B) 3
- C) 2
- D) 1
- Answer: 2



Solution: Potassium permanganate is standardized against pure oxalic acid. It involves a redox reaction. Oxalic acid is oxidised to carbon dioxide by  $\rm KMnO_4$ , which itself gets reduced to  $\rm MnSO_4$ . Oxalic acid reacts with potassium permanganate in the following way.

 $2\,\mathrm{KMnO_4}\ +\ 3\mathrm{H}_2\mathrm{SO_4}\ +\ 5(\mathrm{COOH})_2\ \rightarrow\ \mathrm{K}_2\mathrm{SO_4}\ +\ 2\,\mathrm{MnSO_4}\ +\ 8\mathrm{H}_2\mathrm{O}\ +\ 10\,\mathrm{CO_2}\,\uparrow$ 

The change in oxidation state of carbon per molecule of oxalic acid is 2.

- Q.24. Which oxoacid has maximum oxygen atoms?
- A) Hypophosphorus acid
- B) Ortho phosphoric acid
- C) Pyrophosphoric acid
- D) Phosphonic acid

Answer: Pyrophosphoric acid

Solution:

Hypophosphorous (Phosphinic) acid	$H_3PO_2$
Orthophosphorous (Phosphonic) acid	H <sub>3</sub> PO <sub>3</sub>
Orthophosphoric acid	H <sub>3</sub> PO <sub>4</sub>
Pyrophosphoric acid	$H_4P_2O_7$

Q.25. Find out the number of species having similar bond order.

 $\mathrm{CN}^-\!\!, \, \mathrm{O}_2^{2-}\!\!, \, \mathrm{O}_2^{2+}\!\!, \, \mathrm{O}_2^-\!\!, \, \, \mathrm{NO}$ 

- A) 2
- B) 3
- **C**) 4
- D) 5

Answer:

2

Solution:

Number of $e^-$	Bond order
1	0.5
2	1
3	0.5
4	0
5	0.5
6	1
7	0.5
8	0
9	0.5
10	1
11	1.5
12	2
13	2.5
14	3
15	2.5
16	2
17	1.5
18	1
19	0.5
20	0

 $\rm CN^-$  and  $\rm O_2^{2+}$  are having 14 electrons each, hence the bond order is 3.

Q.26. Consider the following statements:

Statement I:  $\rm KMnO_4,~K_2Cr_2O_7$  and  $\rm Fe^{3+}$  can convert  $\rm I^-$  to  $\rm I_2$  independently.

Statement II: Manganate ion is paramagnetic.



- A) Statement I and II both correct
- B) Statement I is correct and statement II is incorrect
- C) Statement I is incorrect and statement II is correct
- D) Both statement I and II are incorrect
- Answer: Statement I and II both correct
- Solution: lodine is liberated from potassium iodide.

$$\begin{split} 10I^- &+ 2\,MnO_4^- + 16H^+ \to 2\,Mn^{2+} + 8H_2O + 5I_2 \\ & K_2Cr_2O_7 \\ \text{Potassium dichromate} + 7H_2SO_4 + 6KI \to Cr_2(SO_4)_3 + 3I_2 + 4K_2SO_4 + 7H_2O \\ & 2\,Fe^{3+} + 2KI \to 2\,Fe^{2+} + I_2 + 2K^+ \end{split}$$

Manganate ion is paramagnetic in nature with one unpaired electron.

Q.27. 250 g of an aqueous solution contains D-glucose. The % of carbon (by mass) present in the solution is 16.7. Find the molality of the solution.

A) 2.56 m

B) 3.98 m

C) 3.24 m

- D) 1.78 m
- Answer: 3.98 m
- Solution: 1. D-glucose  $C_6H_{12}O_6$

```
2. Molar Mass: 180 g
```

3. C<sub>6</sub>  

$$\downarrow$$
 H<sub>12</sub>O<sub>6</sub>  
72 g of C is 180 g of glucose

Mass of 
$$C = \frac{16.7}{100} \times 250 = 41.75 \text{ g}$$

Mass of D-glucose =  $\frac{180}{72} \times 41.75 = 104.375$  g

Mass of solvent = 145.625 g

Q.28. Consider the following statements:

Statement I: The energy of electron in  $_{2s}$  orbital of  $\mathrm{He^+}$  is more than that of  $\mathrm{Li^{2+}}$ 

Statement II: The energy of an electron in an orbital decreases with increase atomic number.

- A) Both statements are correct and statement II is correct explanation of statement I
- B) Both statements are correct and statement II is not correct explanation of statement I
- C) Statement I is correct and statement II is incorrect
- D) Statement I is incorrect and statement II is correct

Answer: Both statements are correct and statement II is correct explanation of statement I

Solution: Energy of electron in 
$${\rm n}^{th}$$
 orbit of a Bohr atom is,  ${\rm E}_n=-13.6\frac{z^2}{{\rm n}^2}{\rm eV}$ 

Greater the value of atomic number, lesser is the energy.



Q.29. Match List-I consisting of pollutant to List-II consisting of disease

	List I		List II		
Α.	Sulphate $> 500 \text{ ppm}$	Ρ.	Methemoglobinemia		
В.	Nitrate $> 50 \text{ ppm}$	Q.	Mottling of teeth		
С.	Lead > 50 ppb	R.	Laxative effect		
D.	${\sf Fluoride} > 2 ~{ m ppm}$	S.	Kidney damage		

- A) A-P, B-Q, C-R, D-S
- B) A-R, B-P, C-S, D-Q
- C) A-Q, B-R, C-P, D-S
- D) A-Q, B-R, C-S, D-P
- Answer: A-R, B-P, C-S, D-Q
- Solution:  $F^-$  ion concentration above 2 ppm causes brown mottling of teeth. At the same time, excess fluoride (over 10 ppm) causes harmful effect to bones and teeth

Lead: Drinking water gets contaminated with lead when lead pipes are used for transportation of water. The prescribed upper limit concentration of lead in drinking water is about 50 ppb. Lead can damage kidney, liver, reproductive system etc.

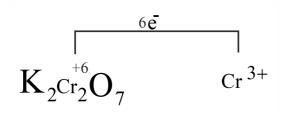
Sulphate: Excessive sulphate  $(>500 \ ppm)$  in drinking water causes laxative effect, otherwise at moderate levels it is harmless.

Nitrate: The maximum limit of nitrate in drinking water is 50 ppm. Excess nitrate in drinking water can cause disease such as methaemoglobinaemia ('blue baby' syndrome).

- Q.30. 10 mL of  $Fe^{2+}$  ion react completely with 20 mL of 0.02 molar acidified  $K_2 Cr_2 O_7$  solution. Find the molarity of  $Fe^{2+}$  ion.
- A) 0.12
- B) 0.24
- C) 0.36
- D) 0.48
- Answer: 0.24
- Solution:

 $Fe^{2+} \longrightarrow Fe^{3+}$ 

n-factor for above equation = 1



 $n_f = 6$ 

 $\left(\mathrm{M}\times\mathrm{n}_{f}\times\mathrm{V}\right)_{Fe^{2+}} = \left(\mathrm{M}\times\mathrm{n}_{f}\times\mathrm{V}\right)_{K_{2}Cr_{2}O_{7}}$ 

$$M\times 10\times 1=0.02\times 20\times 6$$

$$\rm M=0.\,24~M$$

Q.31. Number of basic oxides among the following compounds is:

 $\mathrm{NO}_2,\ \mathrm{N}_2\mathrm{O},\ \mathrm{NO},\ \mathrm{Li}_2\mathrm{O},\ \mathrm{SO}_2,\ \mathrm{PbO}$ 

A) 4



- B) 3
- **C)** 2
- **D**) 1

Answer:

1

- Solution: NO<sub>2</sub>, SO<sub>2</sub> are acidic oxides
  - N<sub>2</sub>O, NO, are neutral oxides
  - ${\rm Li}_2{\rm O}$  is basic oxide
  - PbO is an amphoteric oxide
- Q.32. Assertion: Hydrogen peroxide can act both as an oxidizing agent as well as reducing agent in acidic as well as basic medium.

Reason: Density of  ${\rm H_2O_2}$  is less than that of  ${\rm D_2O}$ 

- A) Both assertion and reason are correct
- B) Assertion is correct and reason is false
- C) Assertion is false and reason is correct
- D) Both assertion and reason is false
- Answer: Assertion is correct and reason is false
- Solution: It acts as an oxidising as well as reducing agent in both acidic and alkaline media. Simple reactions are described below.
  - (i) Oxidising action in acidic medium

$$2\,{\rm Fe}^{2+}({\rm aq}) + 2{\rm H}^+({\rm aq}) + {\rm H_2O_2}({\rm aq}) \rightarrow 2\,{\rm Fe}^{3+}({\rm aq}) + 2{\rm H_2O}\left(l\right)$$

(ii) Reducing action in acidic medium

 $2\,{\rm MnO_4^-} + 6{\rm H^+} + 5{\rm H_2O_2} \,{\rightarrow}\, 2\,{\rm Mn^{2+}} + 8{\rm H_2O} + 5{\rm O_2}$ 

- (iii) Oxidising action in basic medium
- $2\,{\rm Fe}^{2+} + {\rm H_2O_2} \,{\rightarrow}\, 2\,{\rm Fe}^{3+} + 2\,{\rm OH^-}$
- (iv) Reducing action in basic medium
- $\rm I_2 + H_2O_2 + 2\,OH^- \,{\rightarrow}\, 2I^- + 2H_2O \, + \, O_2$

The density of hydrogen peroxide is more than that of heavy water

- Q.33. Which of the following are not methods of purification for metals?
  - (A) Poling,
  - (B) Electrolysis,
  - (C) Liquation,(D) Leaching,
  - (E) Calcination,
  - (F) Distillation
- A) (A), (B) and (C)
- B) (B), (D) and (F)
- C) (D) and (F)
- D) (D) and (E)
- Answer: (D) and (E)



Solution: Poling is a method used to purify metals that have oxidized impurities. It is typically used to purify metals like copper or tin that are in the impure form of a copper oxide or tin oxide. A log of wood which is still green is used to stir the liquid metal.

Electrolytic refining is a technique that is used for the extraction and purification of metals that are obtained by refining methods. The impure metal is used as an anode and the pure metal is used a cathode. Soluble salt from the same metal is used an electrolyte.

Liquation process is used for the purification of the metal, which itself is readily fusible, but the impurities present in it are not, used for the purification of Sn and Zn, and for removing Pb from Zn-Aq alloy.

Leaching is a process widely used in extractive metallurgy where ore is treated with chemicals to convert the valuable metals within into soluble salts while the impurity remains insoluble.

Calcination is the process in which the ore of the metal is heated to high temperature in the absence or limited supply of air or oxygen.

Distillation: This method is used for the purification of metals which possess a low boiling point such as mercury and zinc.



### **Section C: Mathematics**

- Q.34. Let  $a_1, a_2, a_3, \dots, a_n$  be in A.P. The ratio of sum of first five terms to the sum of first nine terms is 5:17. Also  $110 < a_{15} < 120$ . Find the sum of first 10 terms of the A.P (where all  $a_i$  ( $i = 1, 2, 3, \dots, n$ ) are integers)
- A) 330
- **B)** 460
- C) 290
- D) 380
- Answer: 380
- Solution: Let the first term be *a* and common difference be *d*.

Given 
$$\frac{S_5}{S_9} = \frac{5}{17} \Rightarrow \frac{\frac{5}{2}(2a+4d)}{\frac{9}{2}(2a+8d)} = \frac{5}{17}$$

$$\Rightarrow d = 4a$$

Also given  $110 < a_{15} < 120 \Rightarrow a + 14d \in (110, 120) \Rightarrow a = 2$ 

so 
$$d=8$$

Now 
$$S_{10} = \frac{10}{2} (4 + 9 (8)) = 380$$

- Q.35. Let *S* be sample space for 5 digit numbers. If p is probability of a number being randomly selected which is multiple of 7 but not divisible by 5, then 9p is equal to:
- A) 1.0146
- B) 1.2085
- C) 1.0285
- D) 1.1521
- Answer: 1.0285
- Solution: We know that five-digit numbers lie from 10000 to 99999
  - $\therefore n(S) = 90000$

Now the number of numbers which are divisible by  $7 = \frac{90000}{7}$ 

Similarly, the number of numbers which are divisible by 7 and  $5 = \frac{90000}{35}$ 

probability, 
$$p = \frac{\frac{90000}{7} - \frac{90000}{35}}{90000}$$

Required probability, 
$$p = ----$$

$$\Rightarrow p = \frac{4}{35}$$

i.e. 9p = 1.0285

Q.36. Let  $A = \begin{bmatrix} 1 & 2 \\ -2 & -5 \end{bmatrix}$ ,  $\alpha$ ,  $\beta \in R$  such that  $\alpha A^2 + \beta A = 2I$ , where *I* is an identity matrix of order  $2 \times 2$ . Then the value of  $\alpha + \beta$  is equal to:

- A) –10
- B) -6
- C) 6
- **D)** 10
- Answer: 10



Solution:

Given 
$$A = \begin{bmatrix} 1 & 2 \\ -2 & -5 \end{bmatrix}$$

So 
$$A^2 = \begin{bmatrix} 1 & 2 \\ -2 & -5 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ -2 & -5 \end{bmatrix} = \begin{bmatrix} -3 & -8 \\ 8 & 21 \end{bmatrix}$$

Also given  $\alpha A^2 + \beta A = 2I$ 

i.e. 
$$\alpha \begin{bmatrix} -3 & -8 \\ 8 & 21 \end{bmatrix} + \beta \begin{bmatrix} 1 & 2 \\ -2 & -5 \end{bmatrix} = 2 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

-3lpha+eta=2 & -8lpha+2eta=0

Solving both the equations, we get

$$lpha=2,\;eta=8\Rightarrowlpha+eta=10$$

Q.37.  $(p \wedge r) \Leftrightarrow (p \wedge \neg q)$  which is equivalent to  $\neg p$ . Then r will be

A) *p* 

B) ~p

**C**) q

Answer:

q

Solution:

p	q	~ <i>p</i>	~q	$p \wedge q$	$p \wedge \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	$p \wedge q \Leftrightarrow p \wedge  extsf{-}q$
T	Т	F	F	Т	F	F
T	F	F	Т	F	Т	F
F	Т	Т	F	F	F	T
F	F	Т	Т	F	F	Т

We can observe that  $(p \wedge q) \Leftrightarrow (p \wedge {}^{\sim} q) \equiv {}^{\sim} p$ 

Hence,  $r \equiv q$ 

Q.38. The remainder of  $(2021)^{2022} + (2022)^{2021}$  when divided by 7 is

```
A)
      0
B)
      1
      \mathbf{2}
C)
D)
      6
Answer:
            0
             We know 2023 = 7 \times 289
Solution:
             So (2021)^{2022} + (2022)^{2021}
             =(2023-2)^{2022}+(2023-1)^{2021}
             = 7m_1 + 2^{2022} + 7m_2 + (-1)^{2021}
             =7(m_1+m_2)+8^{674}-1
             =7(m_1+m_2)+\left(7+1
ight)^{674}-1
             =7(m_1+m_2)+7m_3+1-1
             =7(m_1+m_2+m_3)
             This is a multiple of 7
```

Hence, remainder is 0

Q.39. Let  $R_1$  and  $R_2$  be two relation defined on  $\mathbb{R}$  by  $aR_1b: ab \ge 0$  and  $aR_2b \Leftrightarrow b \ge a, a, b \in \mathbb{R}$  then the correct statement is:

A) Both  $R_1$  and  $R_2$  are equivalence relations



- B)  $R_1$  is equivalence but  $R_2$  is not
- C)  $R_2$  is equivalence but  $R_1$  is not
- D) Both  $R_1$  and  $R_2$  are not equivalence relations

Answer:  $R_1$  is equivalence but  $R_2$  is not

Solution:  $R_1$  is:

reflexive as  $a^2 \ge 0$ 

symmetric as  $ab \ge 0 \Rightarrow ba \ge 0$ 

tranistive as  $ab \ge 0, \ bc \ge 0 \Rightarrow ac \ge 0$ 

Hence,  $R_1$  is an equivalence relation.

 $R_2$  is:

31

not reflexive as  $b \ge a \Leftrightarrow a \ge b$ 

Hence,  $R_2$  is not an equivalence relation.

Q.40. If 
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
 satisfies  $\left(4\sqrt{\frac{2}{5}}, 3\right)$  and  $e = \frac{1}{4}$ , then  $a^2 + b^2$  is equal to \_\_\_\_\_

Answer:

Solution:

For ellipse 
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
  
eccentricity,  $e = \sqrt{1 - \frac{b^2}{a^2}}$   
i.e.  $\frac{1}{4} = \sqrt{1 - \frac{b^2}{a^2}} \Rightarrow \frac{b^2}{a^2} = \frac{15}{16} \Rightarrow 16b^2 = 15a^2$   
Since  $\left(4\sqrt{\frac{2}{5}}, 3\right)$  lies on the ellipse  
so  $\frac{16 \cdot 2}{5a^2} + \frac{9}{b^2} = 1$   
 $\Rightarrow \frac{16 \cdot 23}{16b^2} + \frac{9}{b^2} = 1$   
 $\Rightarrow \frac{15}{b^2} = 1 = b^2 = 15$   
and  $a^2 = 16$   
 $\therefore a^2 + b^2 = 31$ 

Q.41. The value of  $\cos \frac{2\pi}{7} + \cos \frac{4\pi}{7} + \cos \frac{6\pi}{7}$  is equal to A) -1 B) 1 C)  $\frac{-1}{2}$ D)  $\frac{1}{2}$ E) 0 Answer:  $\frac{-1}{2}$ 



Solution:  $\cos \frac{2\pi}{7}$ 

$$\cos\frac{2\pi}{7} + \cos\frac{2\pi}{7} + \cos\frac{5\pi}{7} \\ = \frac{1}{2\sin\left(\frac{\pi}{7}\right)} \left\{ 2\cos\left(\frac{2\pi}{7}\right)\sin\left(\frac{\pi}{7}\right) + 2\cos\left(\frac{4\pi}{7}\right)\sin\left(\frac{\pi}{7}\right) + 2\cos\left(\frac{6\pi}{7}\right)\sin\left(\frac{\pi}{7}\right) \right\} \\ = \frac{1}{2\sin\frac{\pi}{7}} \left\{ \sin\frac{3\pi}{7} - \sin\frac{\pi}{7} + \sin\frac{5\pi}{7} - \sin\frac{3\pi}{7} + \sin\frac{7\pi}{7} - \sin\frac{5\pi}{7} \right\}$$

Since,  $2\cos A\sin B = \sin (A+B) - \sin (A-B)$ 

 $6\pi$ 

$$= \frac{1}{2\sin\frac{\pi}{7}} \left\{ -\sin\frac{\pi}{7} + \sin\pi \right\}$$
$$= \frac{-1}{2}, \quad (\because \sin\pi = 0)$$

 $4\pi$ 

Aliter:

Since, 
$$e^{i\theta} = \cos \theta + i \sin \theta$$
  

$$\therefore \cos\left(\frac{2\pi}{7}\right) + \cos\left(\frac{4\pi}{7}\right) + \cos\left(\frac{6\pi}{7}\right)$$

$$= \operatorname{Re}\left\{ \operatorname{e}^{\frac{2\pi i}{7}} + e^{\frac{4\pi i}{7}} + e^{\frac{6\pi i}{7}} \right\}$$

$$\operatorname{Re}\left\{ \frac{\left[-1 + \left(1 + e^{2\pi i/7} + e^{4\pi i/7} + e^{6\pi i/7} + e^{-2\pi i/7} + e^{-4\pi i/7} + e^{-6\pi i/7}\right)\right]}{2}$$

$$= \operatorname{Re}\left\{ \frac{-1 + (\operatorname{sum of seven roots of unity})}{2} \right\}$$

$$= -\frac{1 + \theta}{2} = \frac{-1}{2}$$

Let  $f(x) = a \sin \frac{\pi[x]}{2} + [2 - x]$ , where [t] represents the greatest integer value less than or equal, then  $\int_0^4 f(x) dx$  is equal to Q.42. A) -2B) -1C) 0  $\mathbf{2}$ D) Answer: -2 $\int_{0}^{4} f(x) dx = \int_{0}^{1} \left( a\left(\sin 0\right) + 1 \right) dx + \int_{1}^{2} \left( a\left(\sin \frac{\pi}{2}\right) + 0 \right) dx + \int_{2}^{3} \left( a\left(\sin \pi\right) - 1 \right) dx + \int_{3}^{4} \left( a\left(\sin \frac{3\pi}{2}\right) - 2 \right) dx$ Solution: = 1 + a - 1 - a - 2 = -2Q.43.  $\int \frac{(x^2+1)e^x}{(x+1)^2} dx = f(x)e^x + C$ , where *C* is a constant, then  $\frac{d^3f}{dx^3}$  at x = 1 is equal to  $\frac{\frac{3}{4}}{\frac{3}{8}}$  $-\frac{\frac{3}{2}}{\frac{3}{2}}$ A) B) C)  $\frac{7}{8}$ D)  $\frac{3}{4}$ Answer:



Solution:

$$\begin{split} &\int \frac{\left(x^{2}+1\right)e^{x}dx}{(x+1)^{2}} = f(x)e^{x} + C \\ &\int e^{x}\left(\frac{x^{2}-1}{(x+1)^{2}} + \frac{2}{(x+1)^{2}}\right)dx = f(x)e^{x} + C \\ &\int e^{x}\left(\frac{x-1}{x+1} + \frac{2}{(x+1)^{2}}\right)dx = f(x)e^{x} + C \end{split}$$

We know that  $\int e^{x} \left( f(x) + f'(x) 
ight) = e^{x} f(x) + c$ 

Here 
$$f(x) = \frac{x-1}{x+1}$$
 &  $f'(x) = \frac{2}{(x+1)^2}$   
So  $\int e^x \left( \left(\frac{x-1}{x+1}\right) + \frac{2}{(x+1)^2} \right) dx = f(x)e^x + C$   
 $\Rightarrow e^x \left(\frac{x-1}{x+1}\right) + C = e^x f(x) + C$ 

On comparing both sides we get  $f(x) = \frac{x-1}{x+1}$ 

So 
$$f'(x) = \frac{2}{(x+1)^2} \& f''(x) = \frac{-4}{(x+1)^3}$$
  
 $f'''(x) = \frac{12}{(x+1)^4}$ ,  
Now  $f'''(1) = \frac{12}{(1+1)^4} = \frac{12}{16} = \frac{3}{4}$ 

- If A is a  $3 \times 3$  matrix with elements from  $\{-1, 0, 1\}$ , then the number of matrices A such that the sum of diagonal elements of Q.44.  $AA^T$  is 6 is
- ${}^{9}C_{3}(2)^{6}$ A)
- ${}^{9}C_{2}(2)^{7}$ B)
- ${}^{9}C_{6}(2)^{3}$ C)

D) 
$${}^{9}C_{3}{}^{9}C_{6}$$

Answer:  ${}^9C_3(2)^6$ 

Solution:  
Let 
$$A = \begin{bmatrix} a & b & c \\ l & m & n \\ p & q & r \end{bmatrix}$$

then  $a^2 + b^2 + c^2 + l^2 + m^2 + n^2 + p^2 + q^2 + r^2 = 6$ 

Hence, total number of matrices will be  ${}^{9}C_{3}(2)^{6}$  as only three places to be filled with 0 and six places with either of -1/1

Q.45. The number of points where tangents are vertical or horizontal to curve  $y^5 + 9xy - 2x = 0$ , are equal to \_\_\_\_\_\_.

A)  $0, \frac{5}{18}$  $0, \frac{5}{15}$ B) C)  $0, \frac{4}{18}$ D)  $0, \frac{4}{15}$ Answer:  $0, \frac{5}{18}$ 



