



Real numbers - Points to Remember

1. Euclid's division lemma:

For given positive integers a and b there exist whole numbers q and r satisfying $a=bq+r$, $0 \leq r < b$.

2. Euclid's division algorithm:

To compute the H.C.F. of two positive integers say a and b , with $a > b$ by using Euclid's algorithm we follow the following steps:

STEP I: Apply Euclid's division lemma to a and b and obtain whole numbers q_1 and r_1 such that $a=bq_1+r_1$, $0 \leq r_1 < b$.

STEP II: If $r_1=0$, b is the H.C.F. of a and b .

STEP III: If $r_1 \neq 0$, apply Euclid's division lemma to b and r_1 and obtain two whole numbers q_2 and r_2 such that $b=q_2r_1+r_2$.

STEP IV: If $r_2=0$, then r_1 is the H.C.F. of a and b .

STEP V: If $r_2 \neq 0$, then apply Euclid's division lemma to r_1 and r_2 and continue the above process till the remainder r_n is zero. The divisor at this stage i.e. r_{n-1} , or the non-zero remainder at the previous stage, is the H.C.F. of a and b .

3. The Fundamental Theorem of Arithmetic:

Every composite number can be expressed (factorised) as a product of primes, and this factorisation is unique except for the order in which the prime factors occur.

Every composite number can be uniquely expressed as the product of powers of distinct primes in ascending or descending order.

4. Properties of Prime Numbers:

(i) There are infinitely many positive primes.

(ii) A positive integer n is prime, if it is not divisible by any prime less than or equal to n .

(iii) If p is a positive prime, then p is an irrational number.

5. Terminating Decimal:

Let $x=\frac{p}{q}$ (where p, q are integers and $q \neq 0$) be a rational number, such that the prime factorisation of q is of the form $2^m \times 5^n$ where m, n are non-negative integers. Then, x has a terminating decimal expansion which terminates after k places of decimals, where k is the larger of m and n .

6. Non-terminating Decimal:

Let $x=\frac{p}{q}$ (where p, q are integers and $p, q \neq 0$) be a rational number, such that the prime factorisation of q is not of the form $2^m \times 5^n$, where m, n are non-negative integers. Then, x has a non-terminating repeating decimal expansion.